

PAPER

HELPER

Conversions, Divisions
and Shapes

Collected, edited and diagrammed
by Guy Loel

Acknowledgment

In this booklet we tried to collect the major tools an origami folders needs when folding a model which does not start from a square.

How to convert a square to US letter size, or to make a clean duo color A4 from Kami are two examples.

We collected techniques from people and sites, and we wish to thank them for developing those.

Joseph Wu

Douglas Philips

Maria Sinayskaya

Thoki Yenn

Origami Resource Center

We are sorry if we missed anyone, please contact us and we will rectify it immediately.

Furthermore, this will be an ongoing project, as we will continue to add more and more tools, such as n-side polygons, for $n=7$ to 12. If you have requests for other tools, please send us an email to iorigamiproductions@gmail.com

As our valued member, you will get this booklet as part of our future events.

We thank you for sharing your love for origami with us, and we are sure you will find this booklet useful.

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Paper Conversions

In origami, most of the time, we use square papers which are really easy to come by. It is also pretty simple to cut a square in case we run out of Kami papers, but once in a while we may need a paper with different proportion. These are the most common rectangles we usually need:

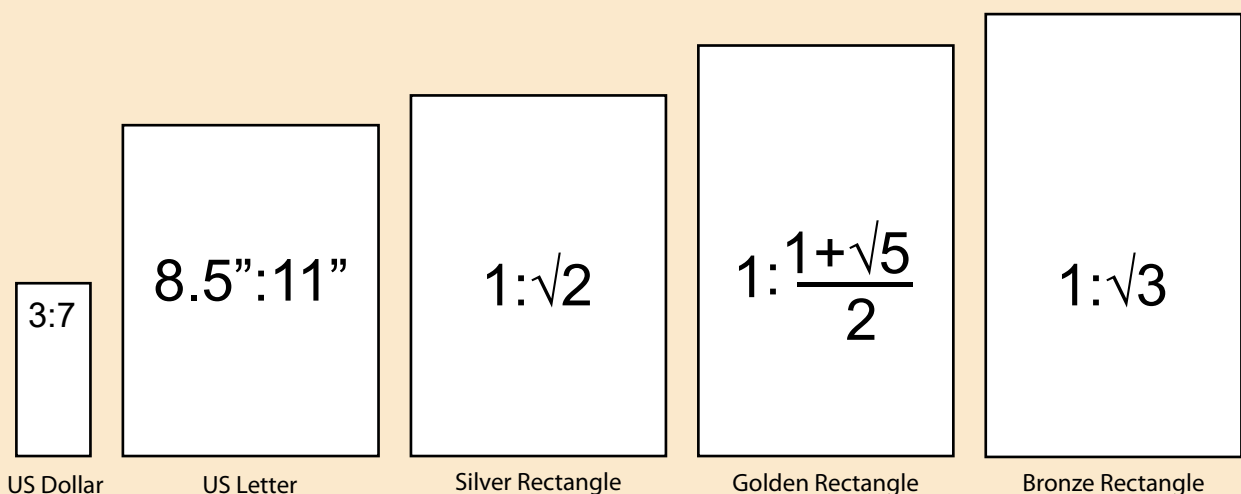
US Dollar Bill

Letter

Silver Rectangle

Golden Rectangle

Bronze Rectangle



US Dollar

US Letter

Silver Rectangle

Golden Rectangle

Bronze Rectangle

US Dollar Bill Proportions

Money Origami is the art of folding dollars into various shapes and designs. Creating origami with money is great for those looking to gift money more creatively.

US dollar bill dimensions are 6.14 " × 2.61" (156.1mm x 66.3mm). Its ratio of length to width is approximately 7:3.



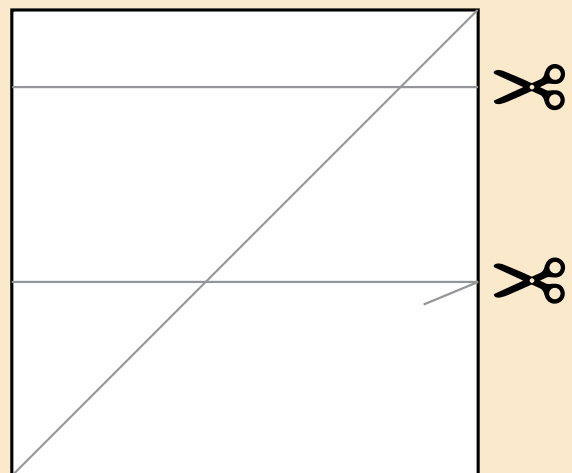
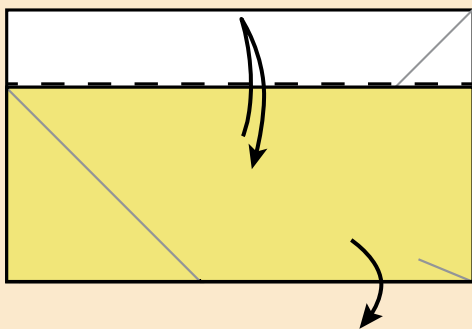
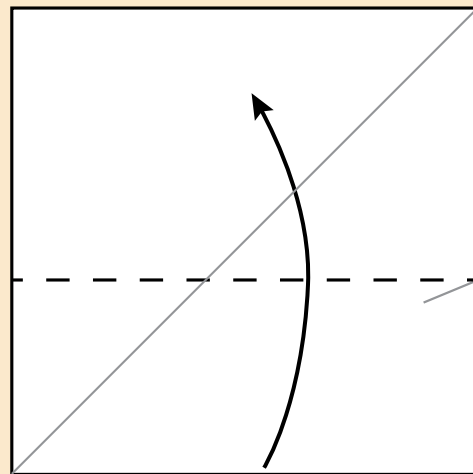
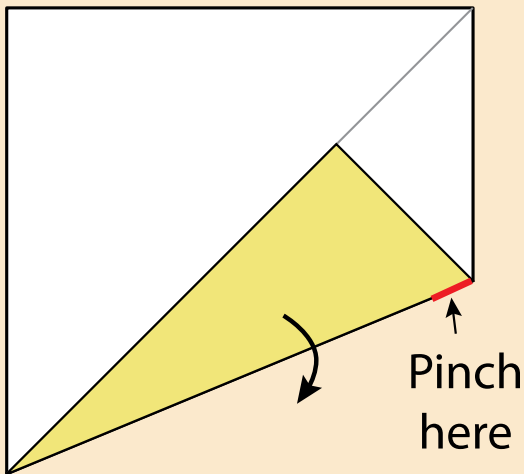
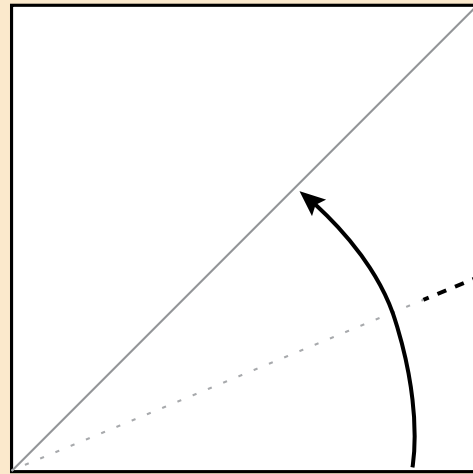
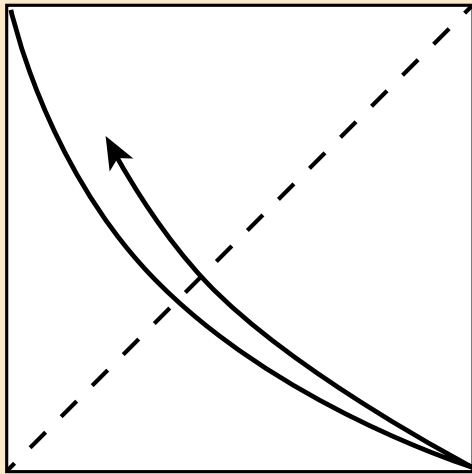
7:3

US Dollar

For practice purposes, it is useful to make rectangles of the same proportion as a dollar bill. These sheets are larger and will allow you to “save” your dollar bills for your final fold.

In the following chapter we will convert square and rectangle papers into US dollar proportions rectangles.

US Dollar Bill from a Square



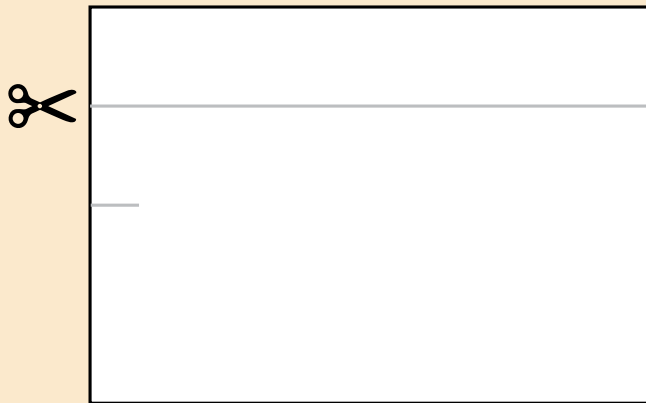
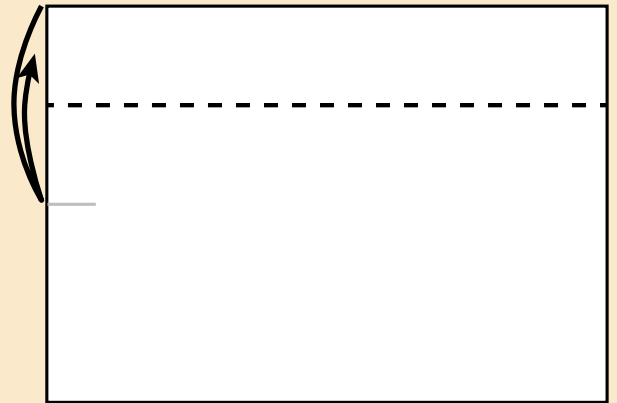
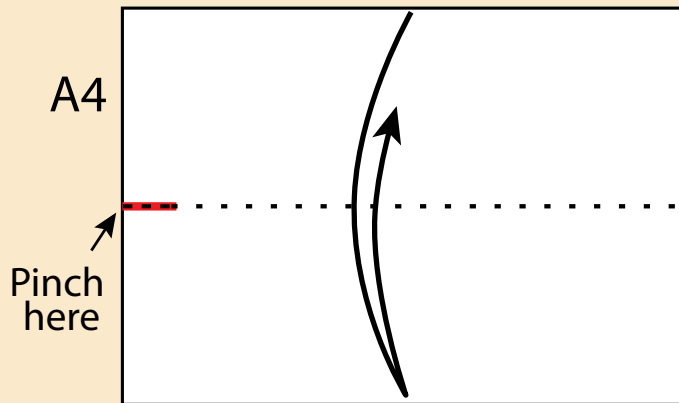
Discard

Dollar bill ratio
7:3

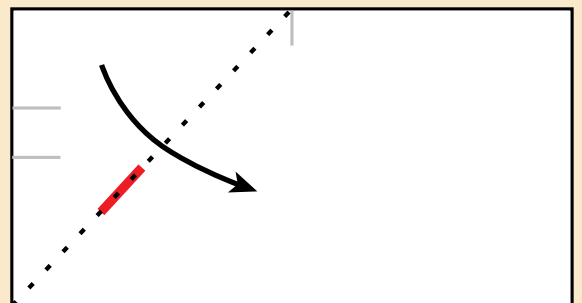
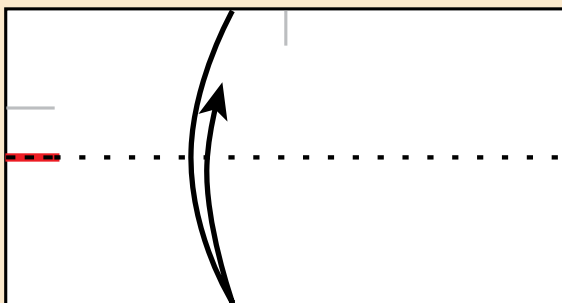
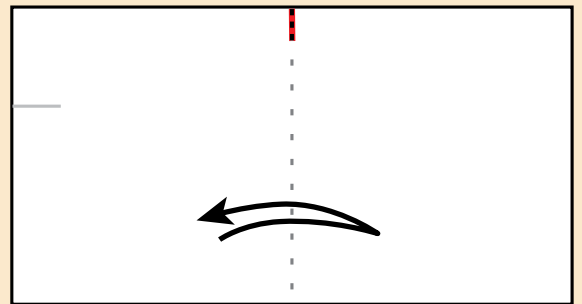
Dollar bill ratio
7:3

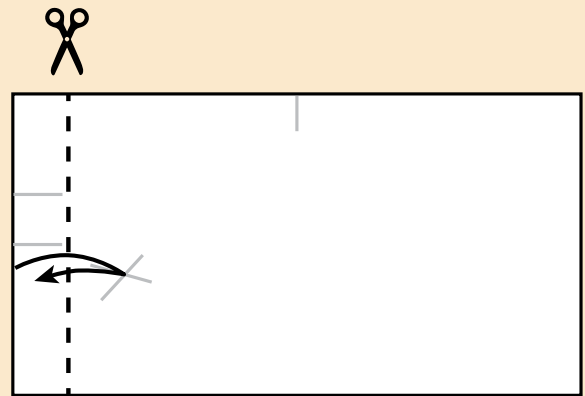
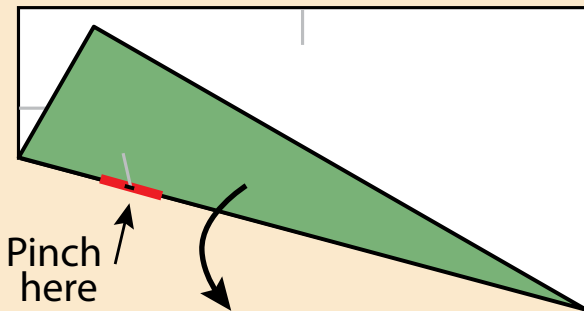
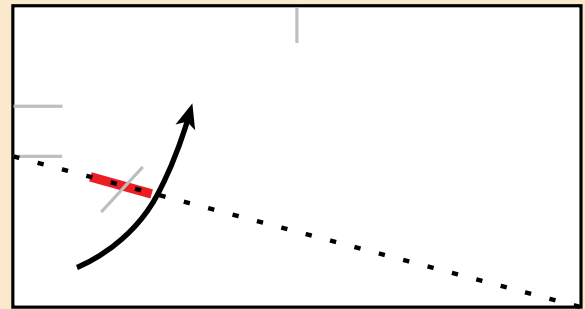
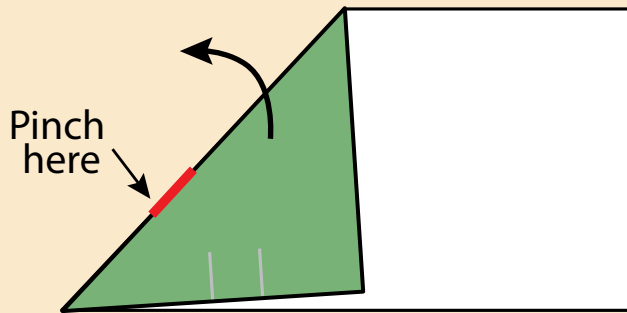


US Dollar Bill from A4

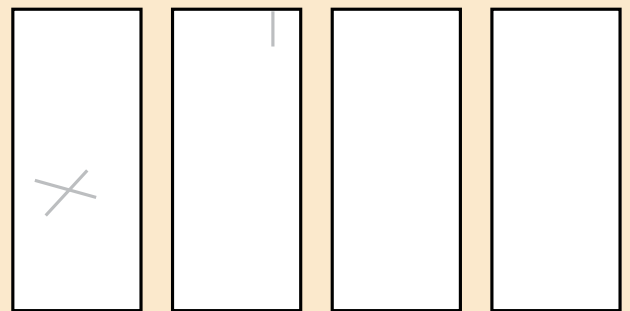
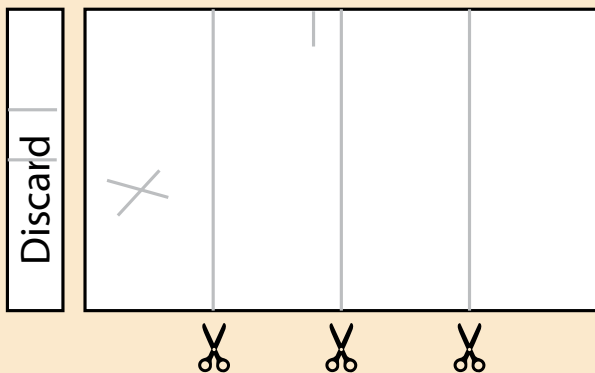


Discard





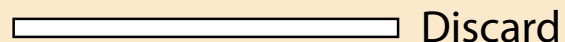
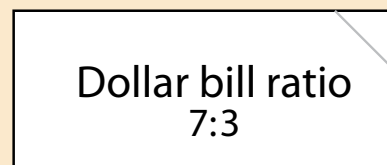
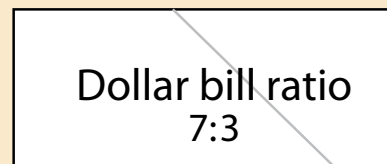
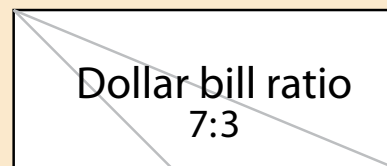
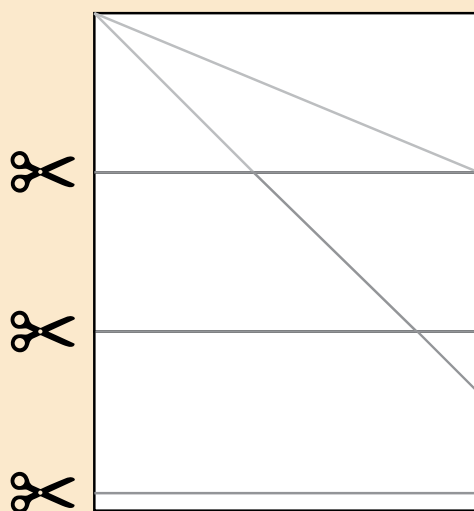
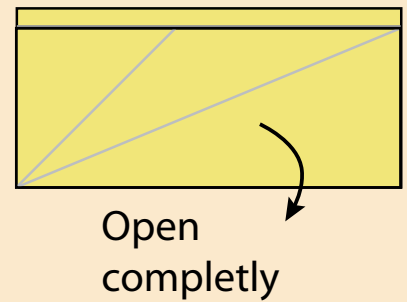
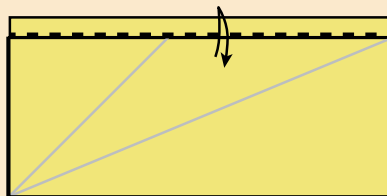
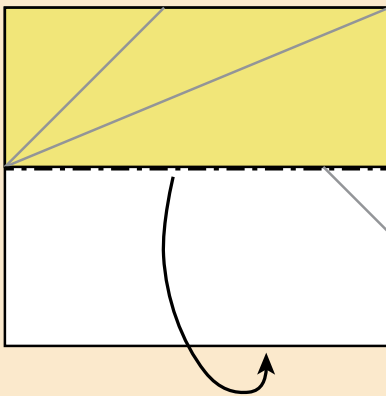
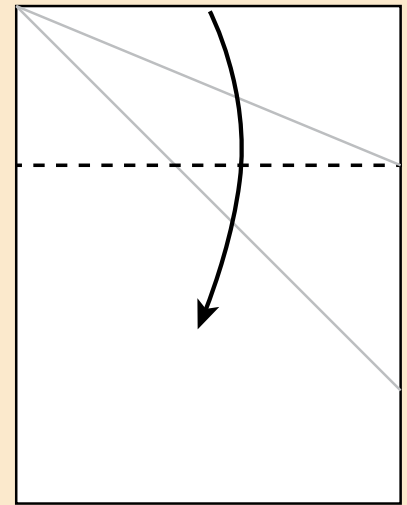
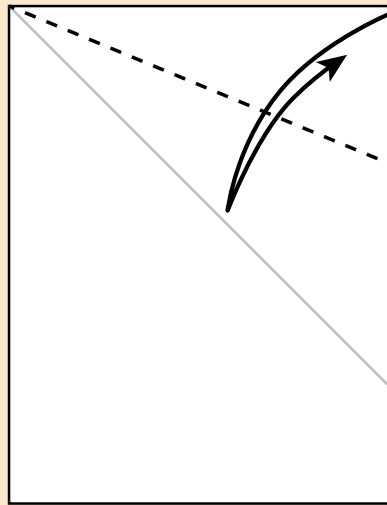
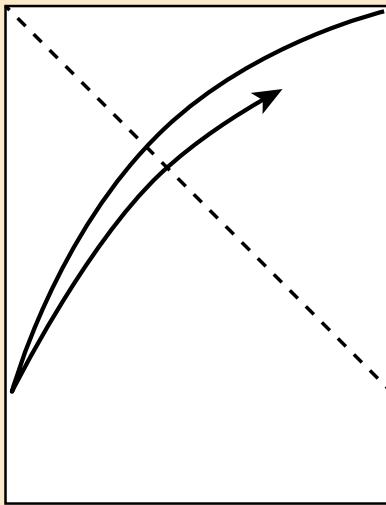
Divide into 4 equal parts



* The resulting 4 sheets are an actual dollar bill size.



US Dollar Bill from Letter-Sized Paper

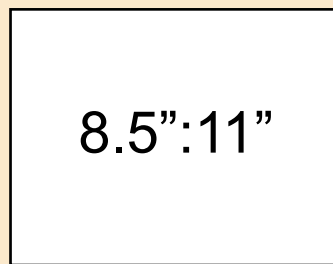


* The result is 7:3 in ratio but bigger than an actual dollar bill



Letter Paper Size

(ANSI) Letter is a paper-size standard defined by the **American National Standards Institute**. It is commonly used in the US and Canada. It measures 8.5 by 11 inches (215.9 by 279.4 mm) and is similar in use to the A4 paper standard used by most other countries.



US Letter

Special Property

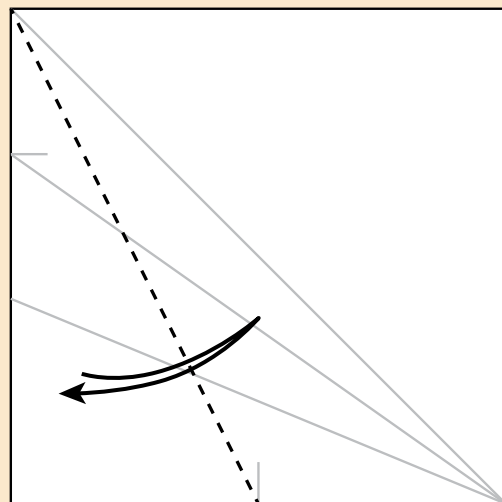
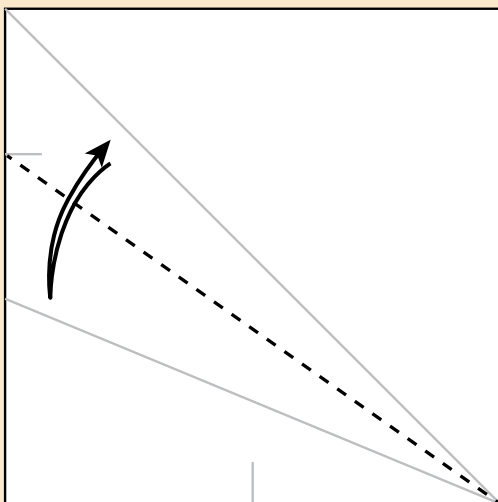
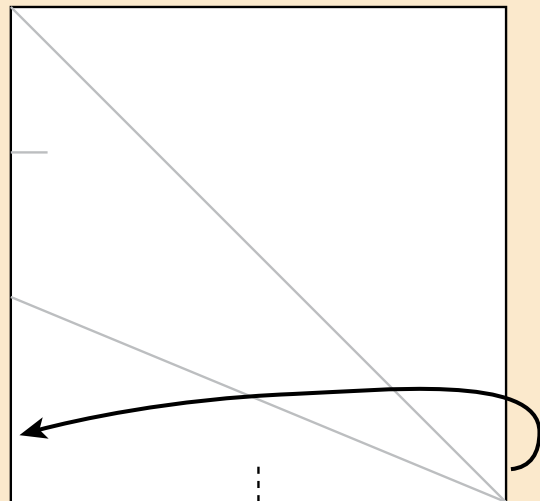
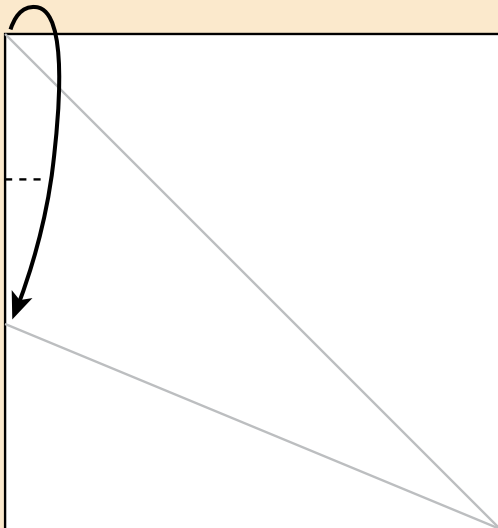
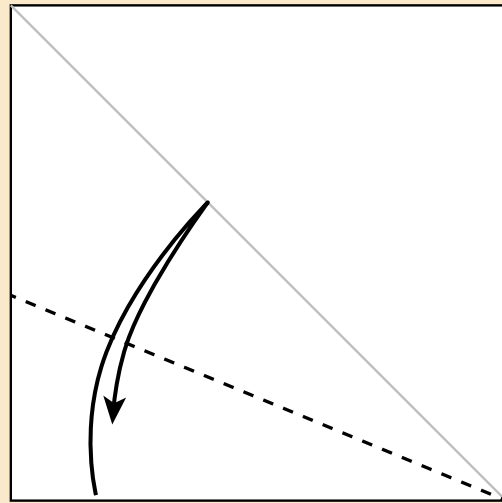
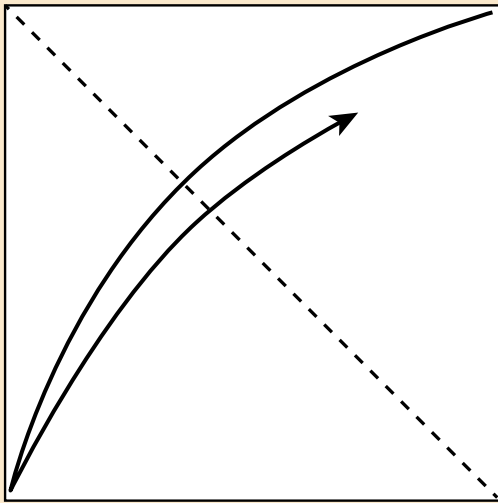
Although there is no special property to this ratio American still loves it.

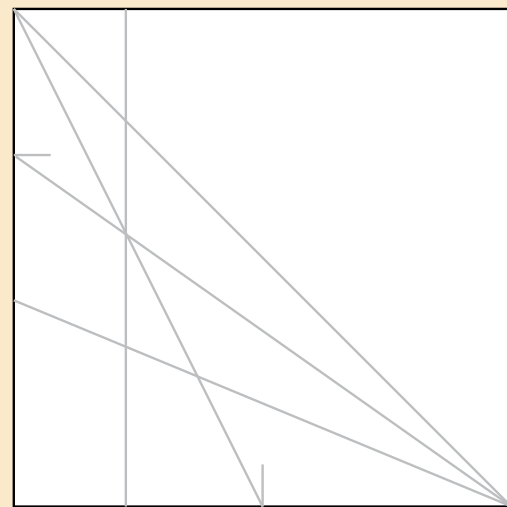
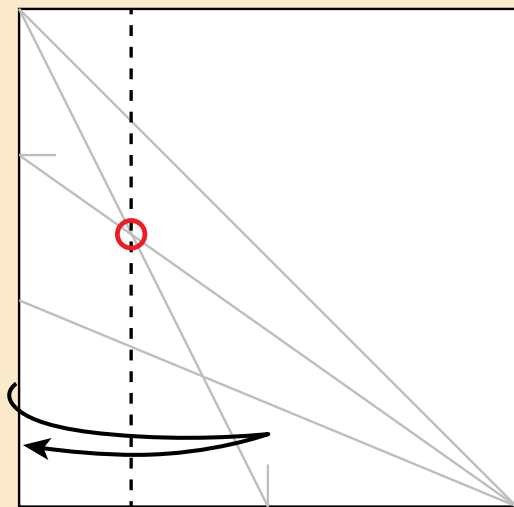
**The precise origins of the dimensions of US letter-size paper are unknown.*

In the following chapter we will convert square and rectangle papers into US Letter proportions rectangles.

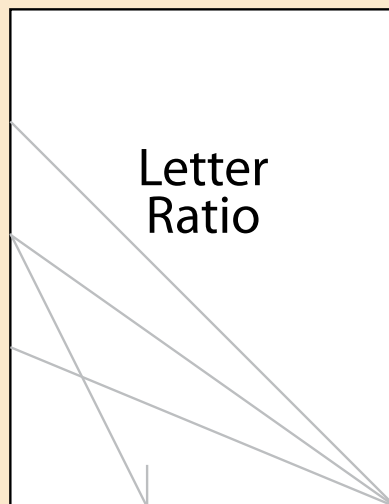
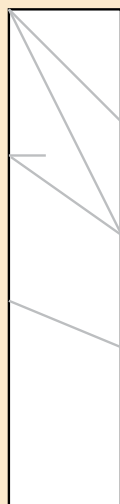
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Letter-Size from a Square

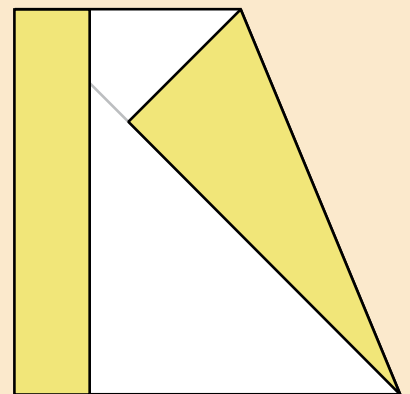
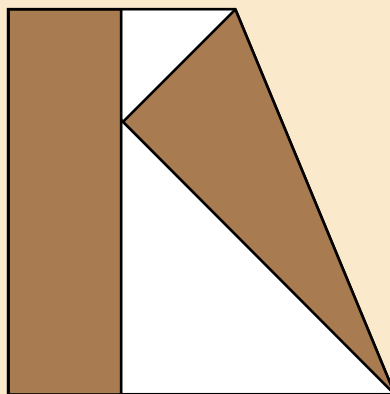
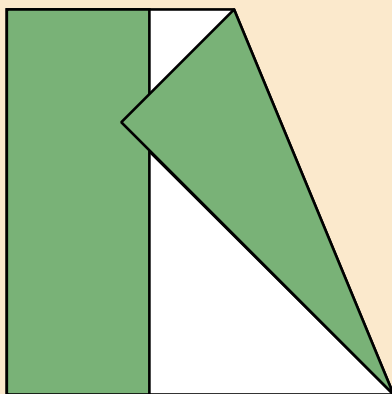
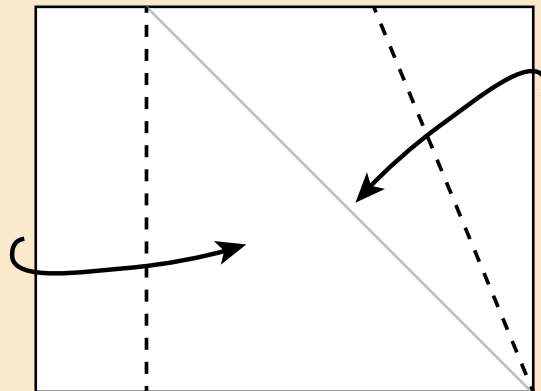
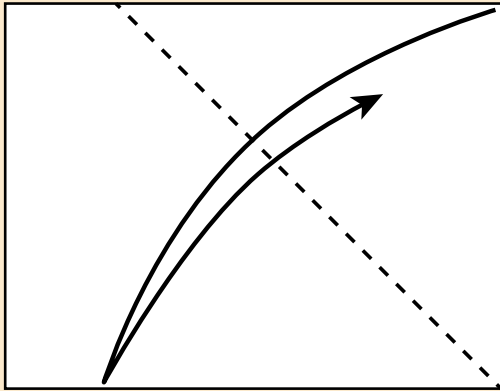


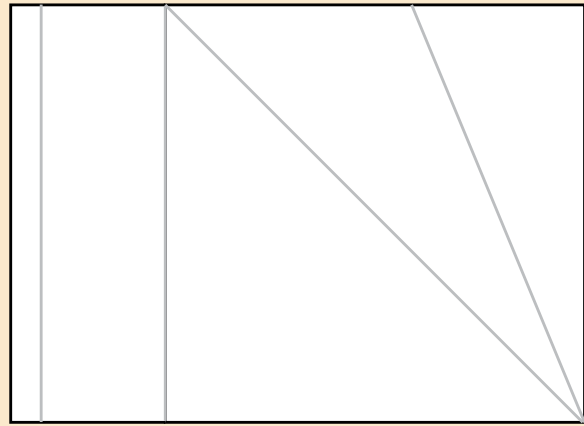
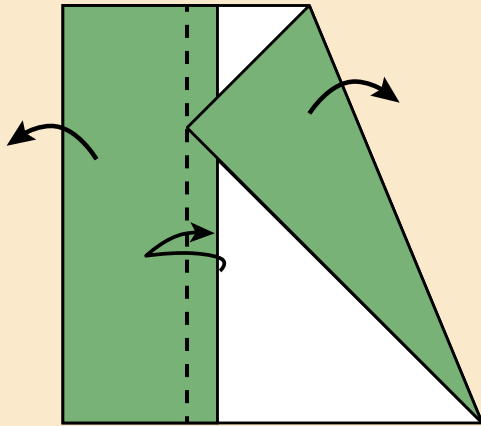


Discard

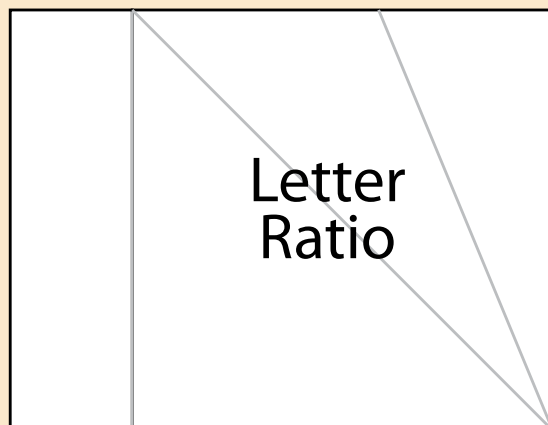
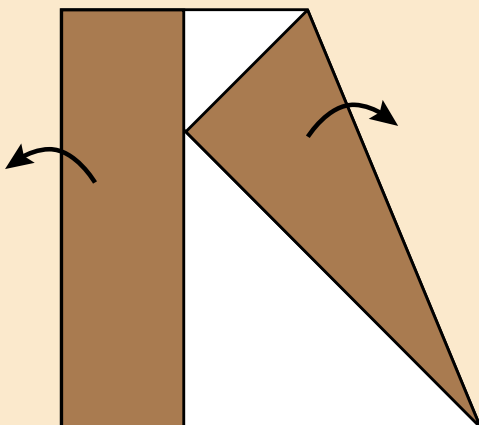
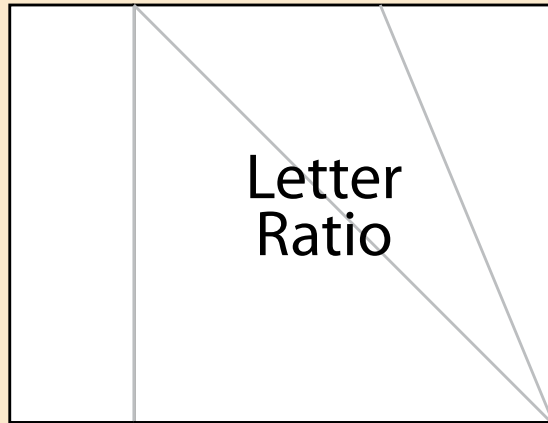


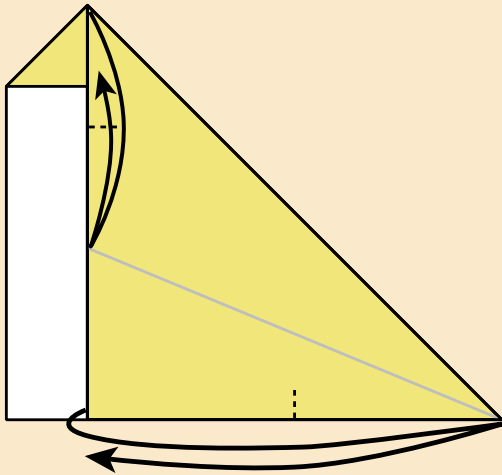
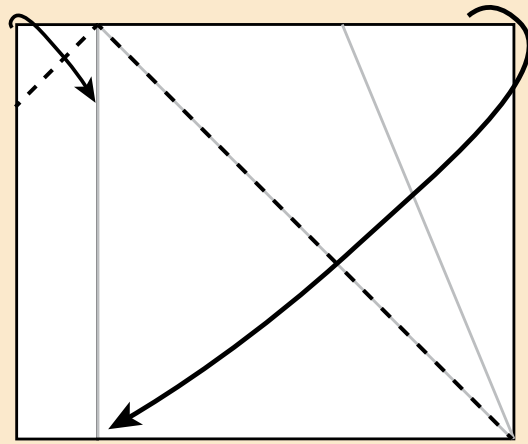
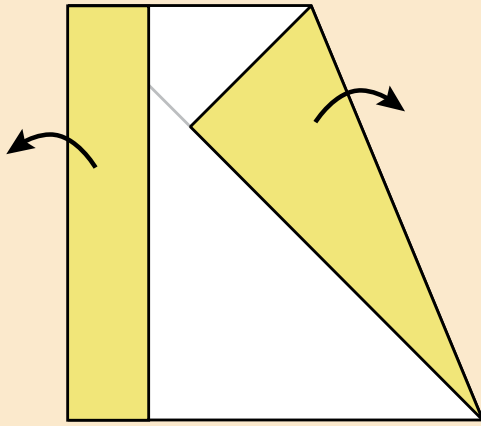
Letter-Size from any Rectangle



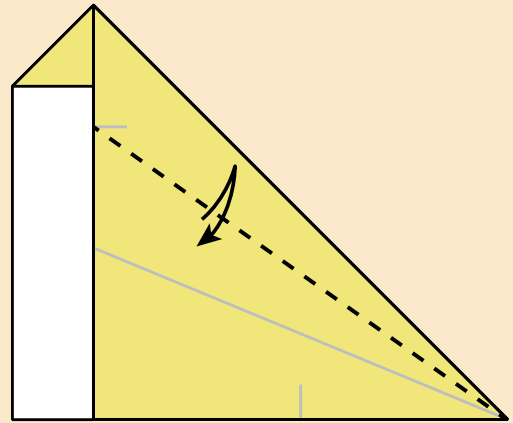


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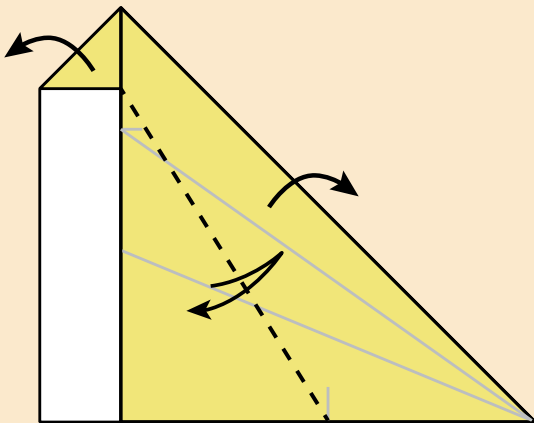




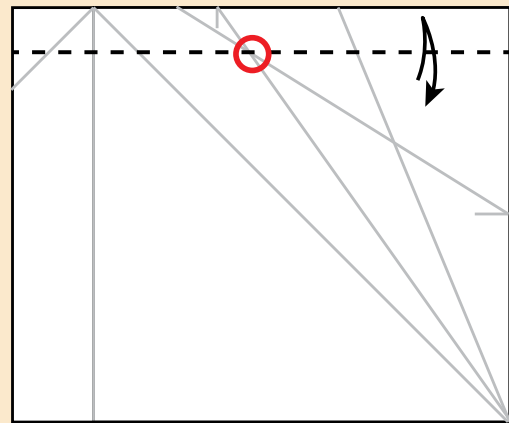
Crease top layer only



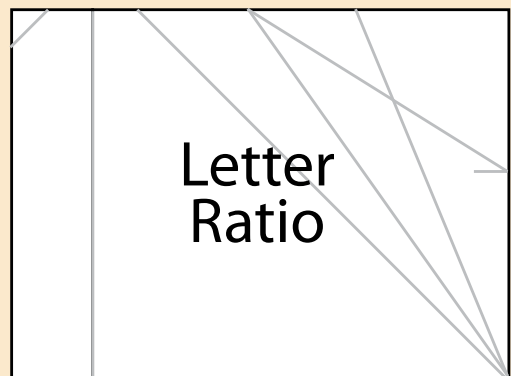
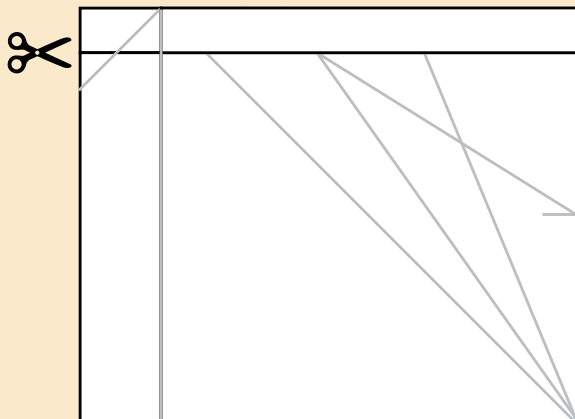
Crease top layer only



Crease top layer only



Discard

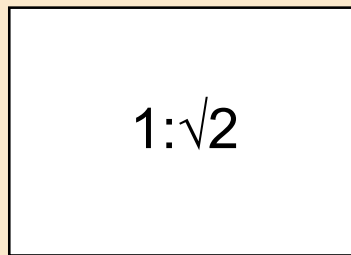


Letter
Ratio



Silver Rectangles (A-Ratio Paper)

The International Standard A-series papers are used around the world with the exception of the USA and Canada. The A-series papers are examples of silver rectangles and have width to length ratios of 1 to $\sqrt{2}$.

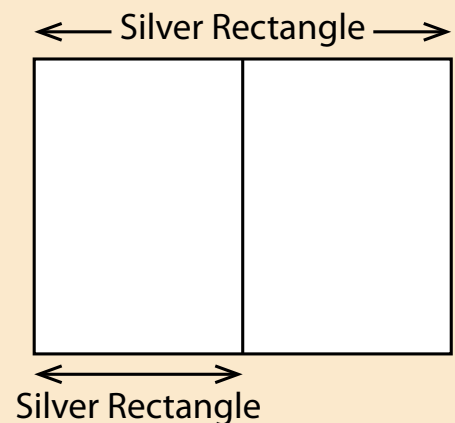


Silver Rectangle

Special Property

If you cut the paper in half crosswise, the two resulting pieces are also of the ratio $1:\sqrt{2}$.

If you cut the A4 in half, the pieces are now called A5. You can cut the paper in half repeatedly and the resulting rectangles will all have the silver ratio.

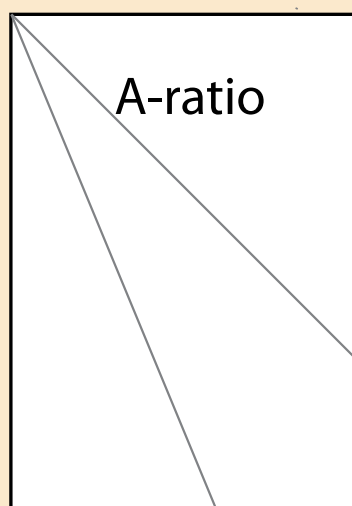
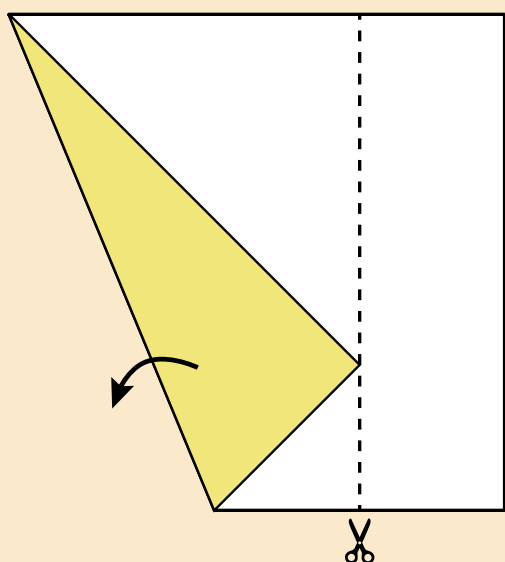
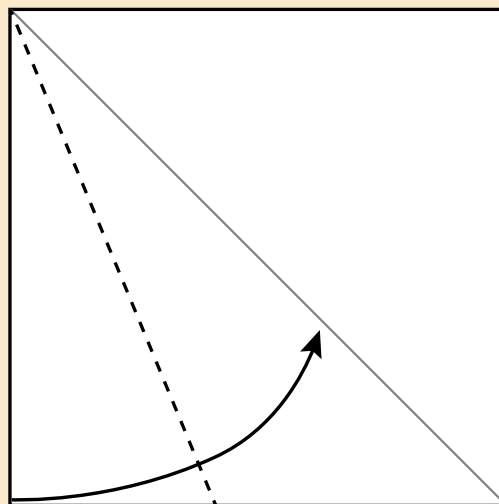
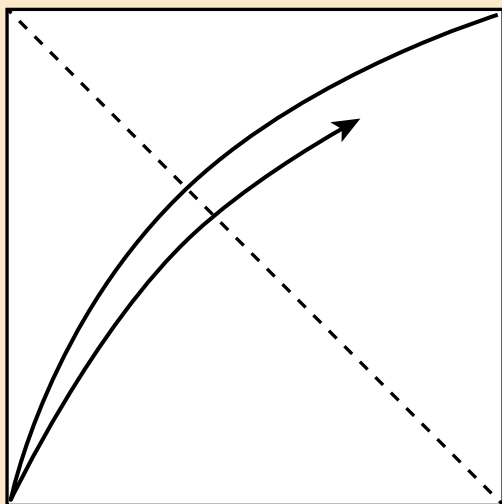


Some origami models use A-size paper instead of a square.

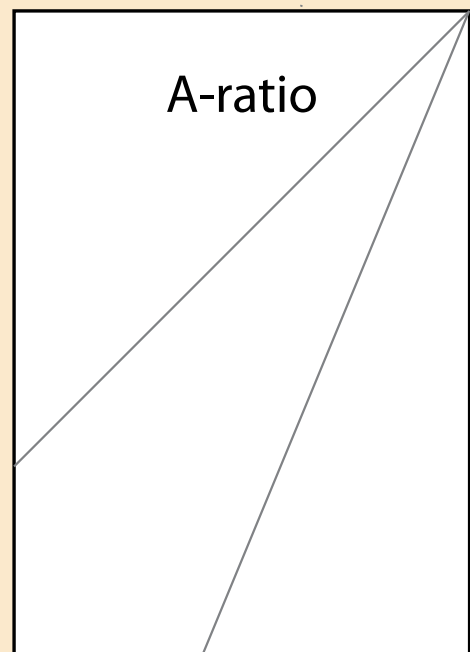
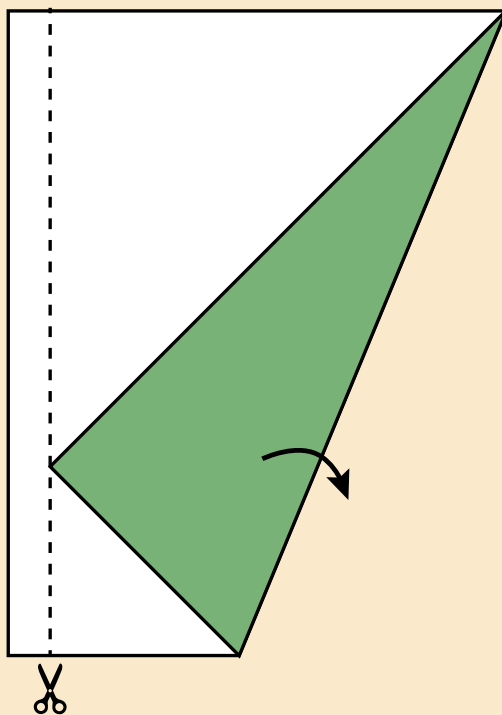
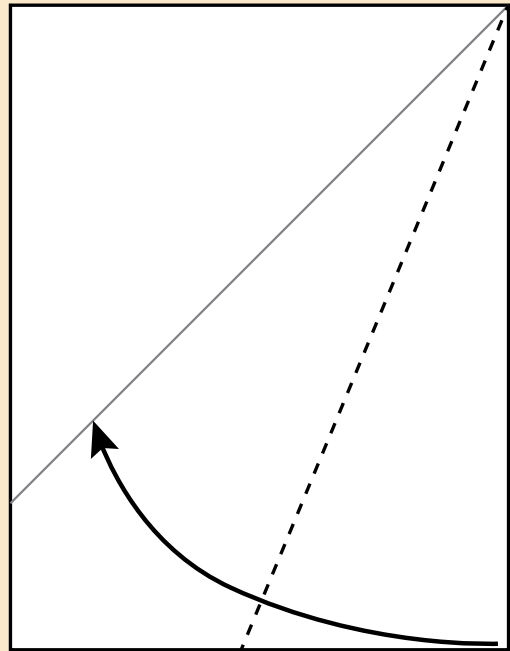
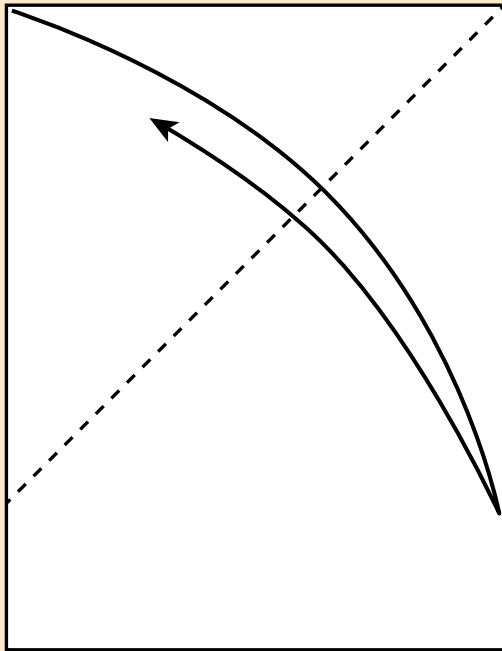
In the USA and Canada, A-series papers are hard to come by. The rest of the world use the A4 paper mostly as copy/printer paper so a duo colour A-size is also hard to find.

In the following chapter we will use square Kami or rectangle craft to get duo-colored A-size papers.

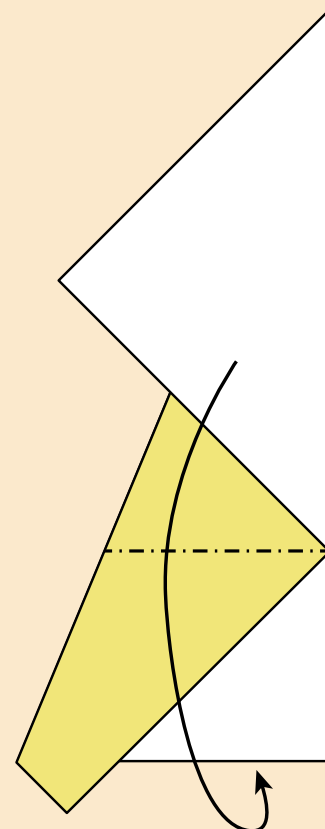
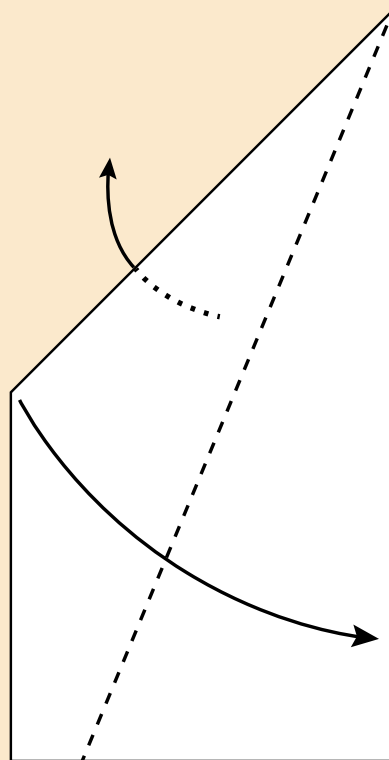
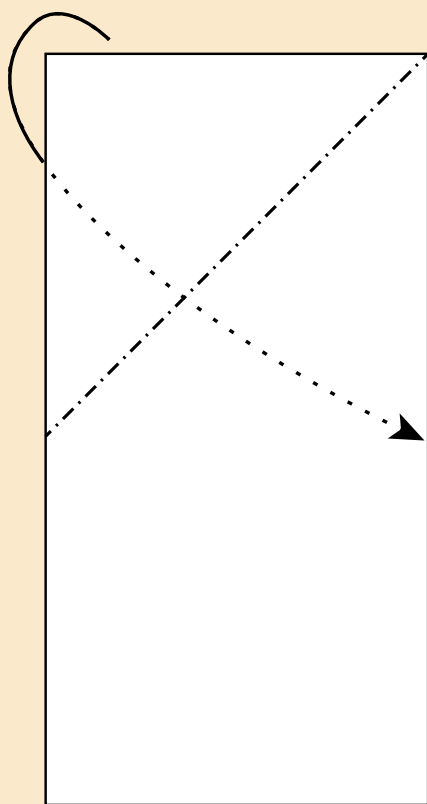
Silver Rectangle from a Square



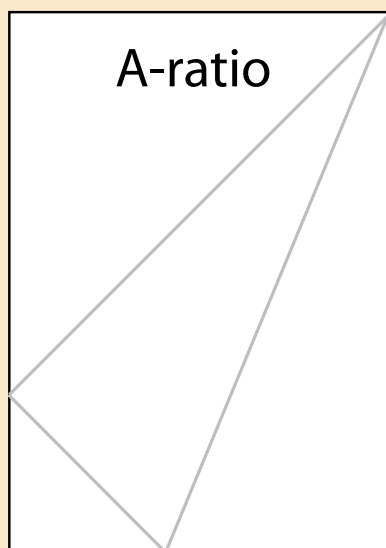
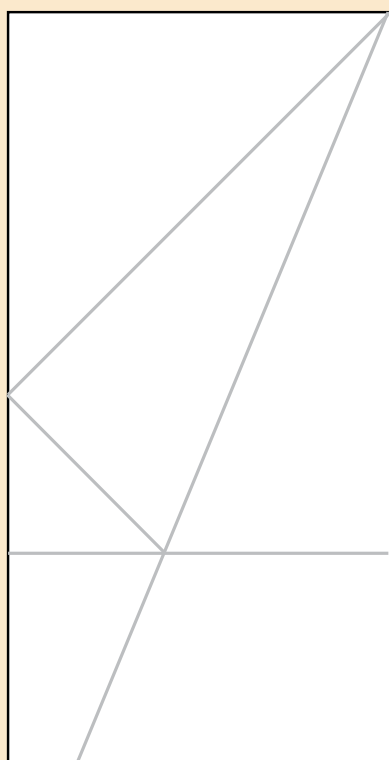
Silver Rectangle from Letter-Sized Paper



Silver Rectangle from a Long Rectangle



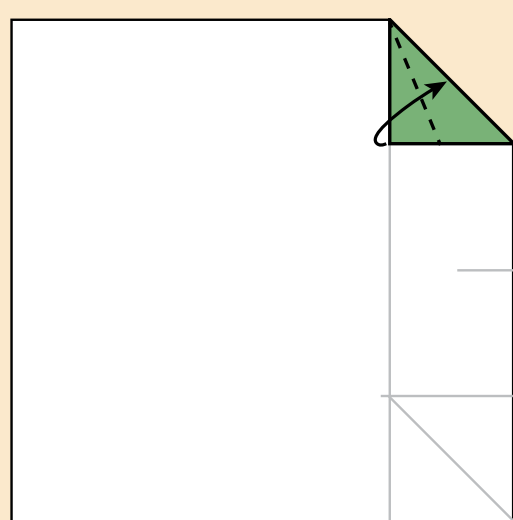
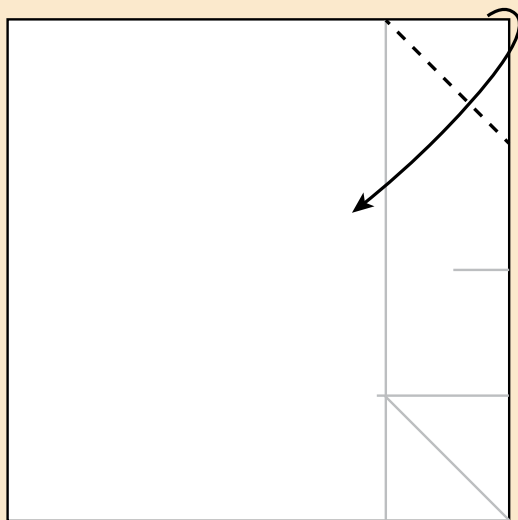
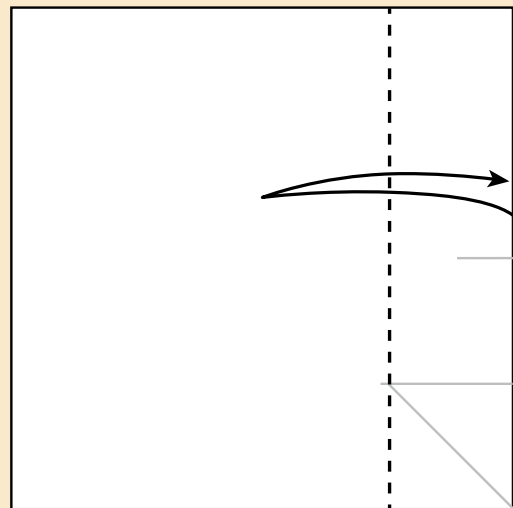
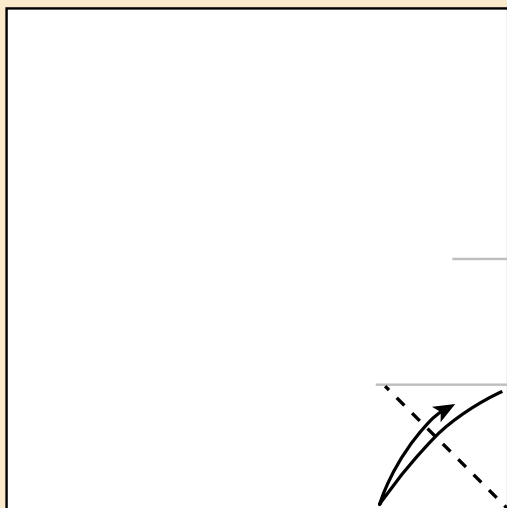
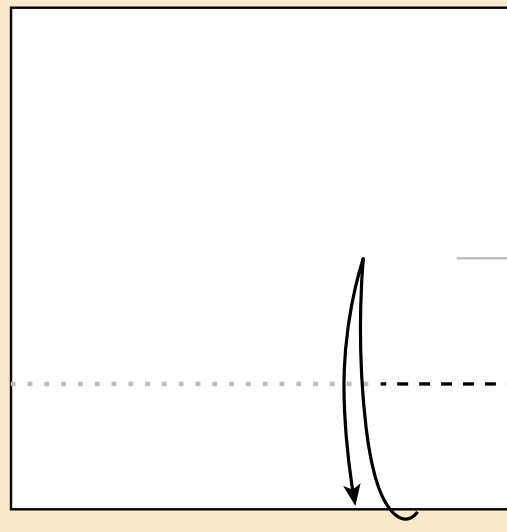
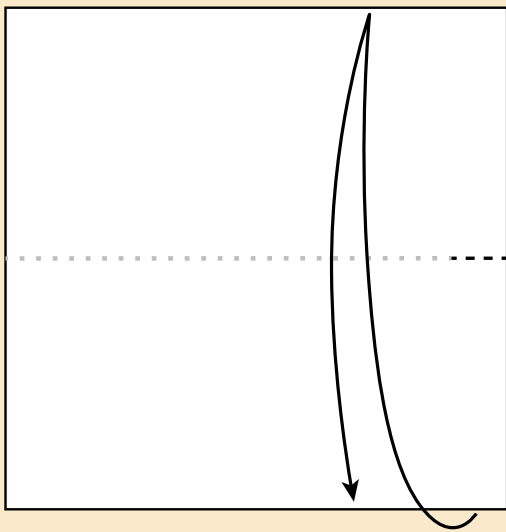
Fold and open all

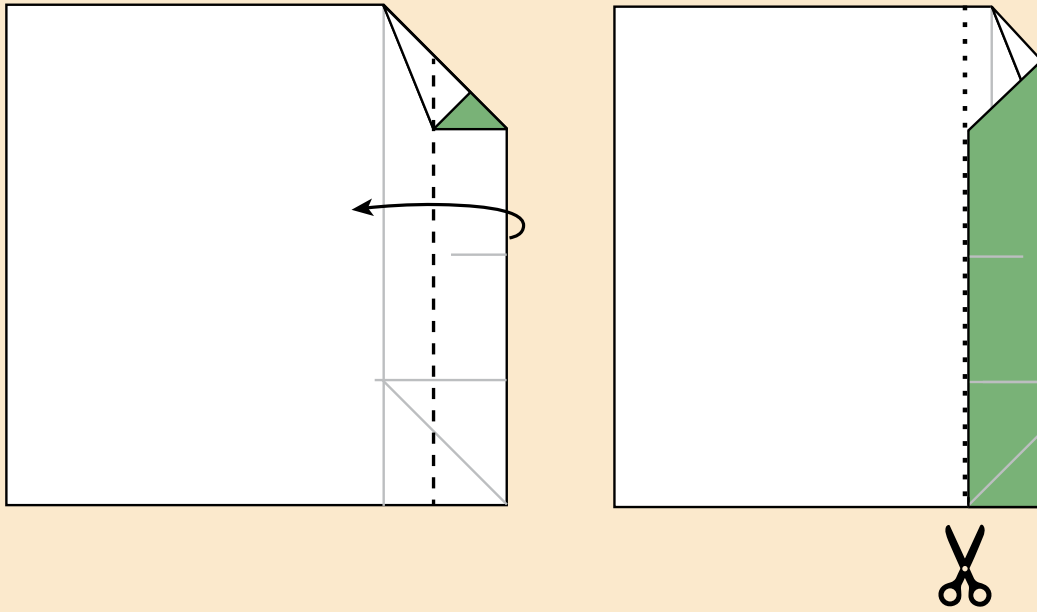


Discard



Creaseless Silver Rectangle from a Square

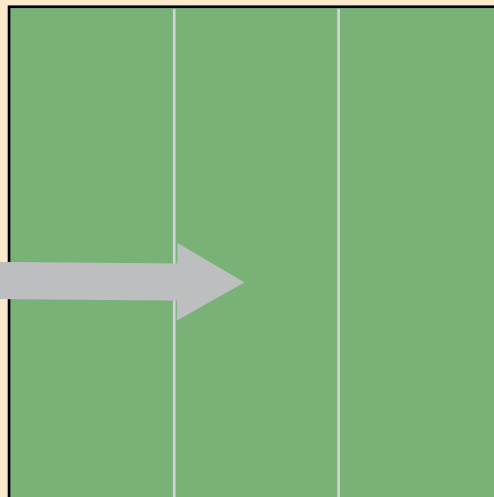
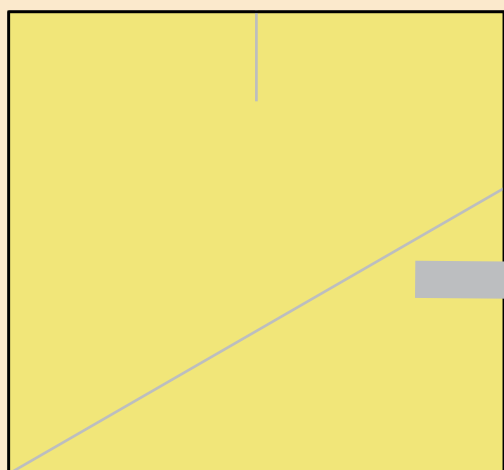
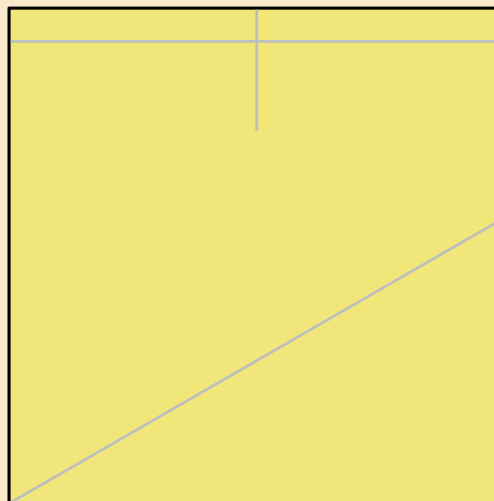
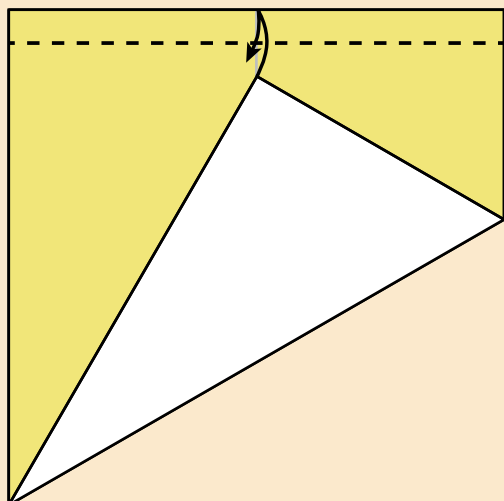
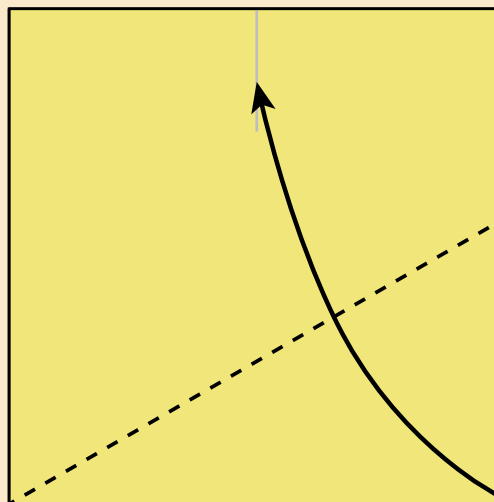
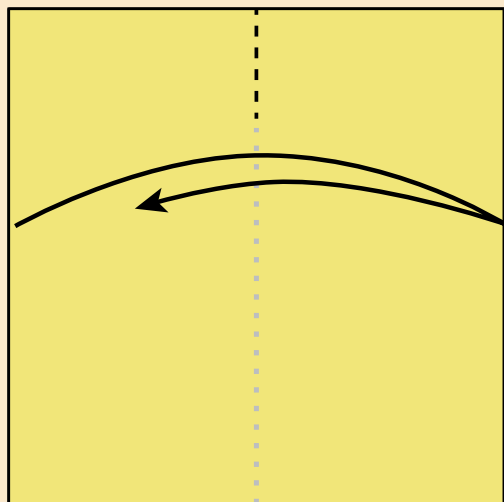




Clean
A-ratio

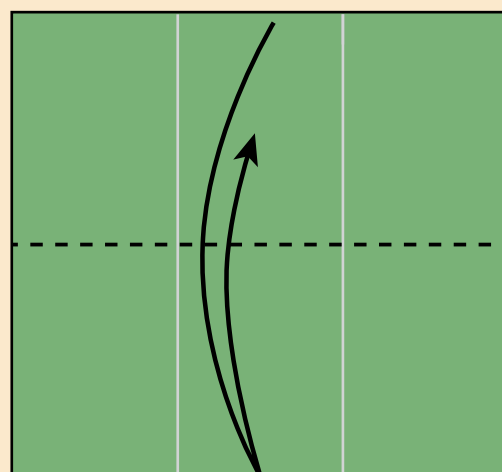
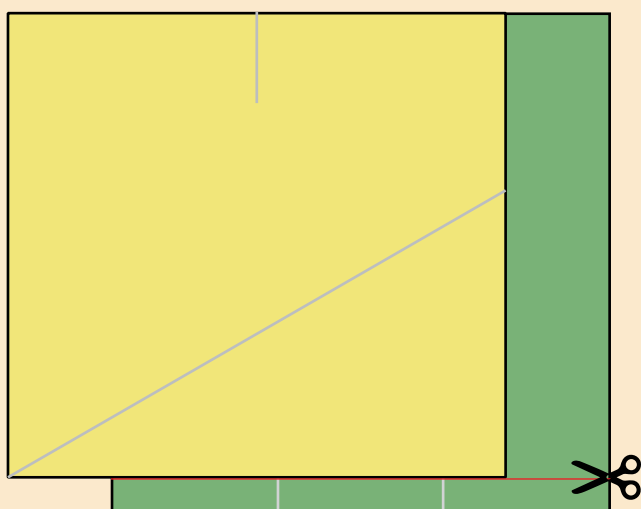


Creating 6 Silver Rectangles from a Square

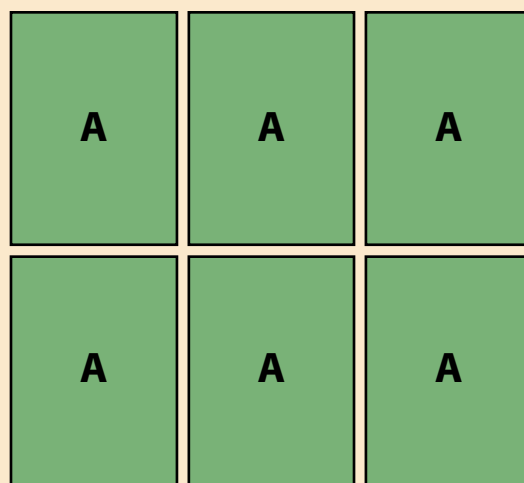
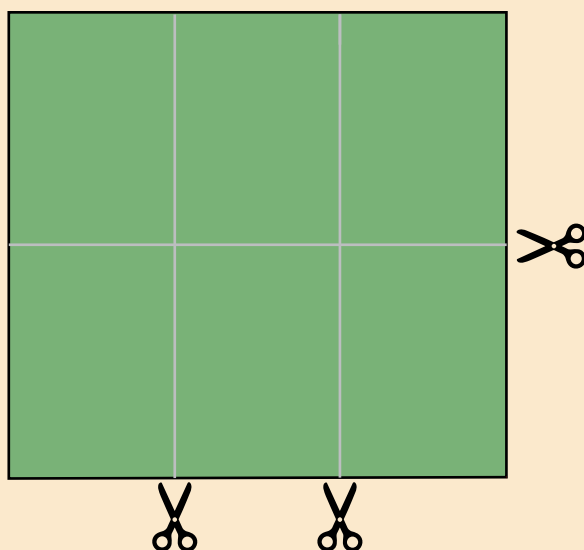


Place the template on a second sheet divided into thirds





Cut the second sheet
according to the template



Golden Rectangle

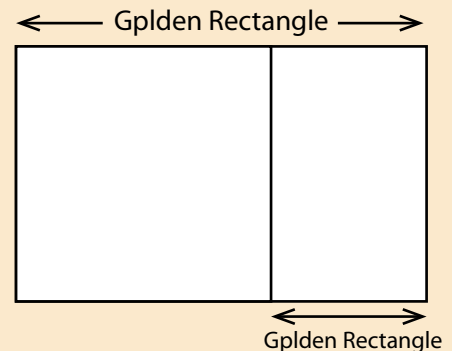
The golden rectangle is not commonly used in origami.
The ratio of the sides is 1:1.61 or in fraction format:

$$1:\frac{1+\sqrt{5}}{2}$$

Golden Rectangle

Special Property

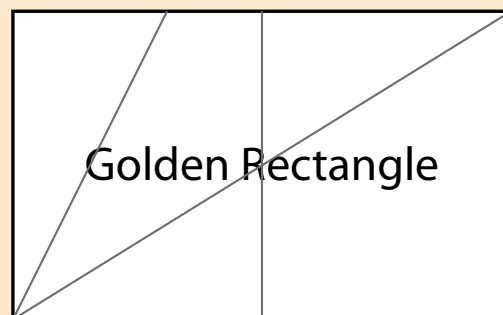
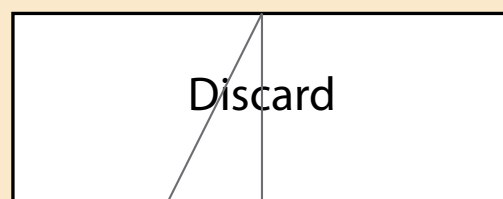
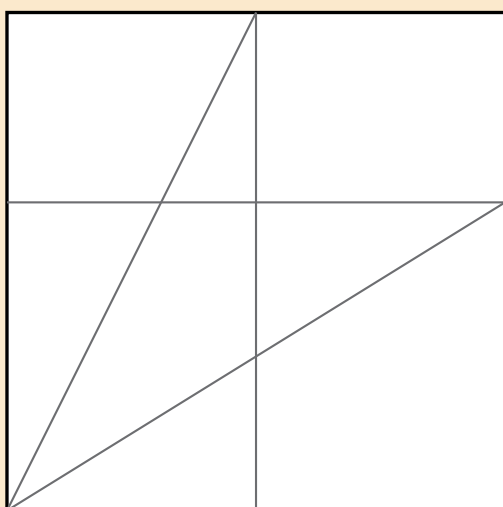
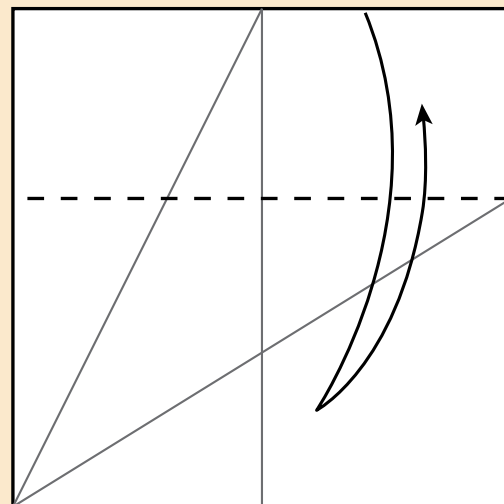
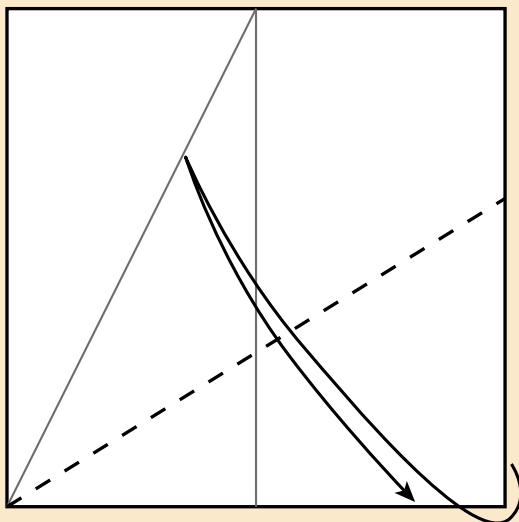
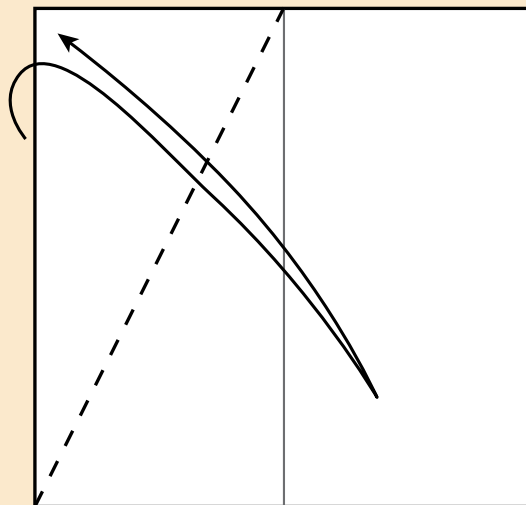
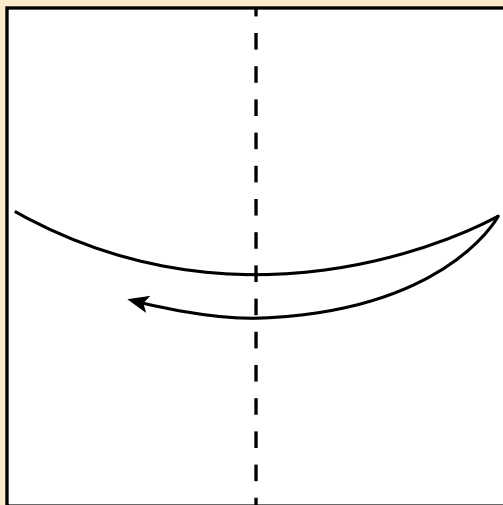
If you remove a square from a golden rectangle, the left-over shape is also a golden rectangle with ratio 1:1.61.



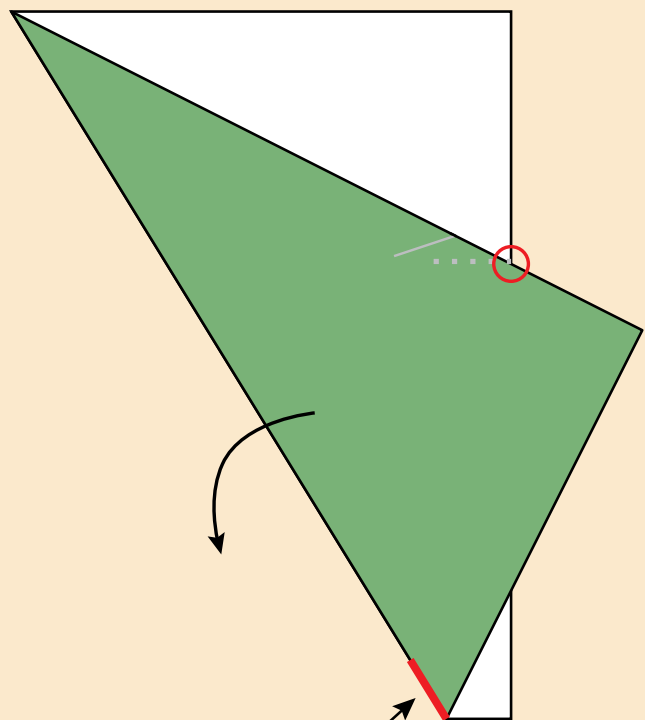
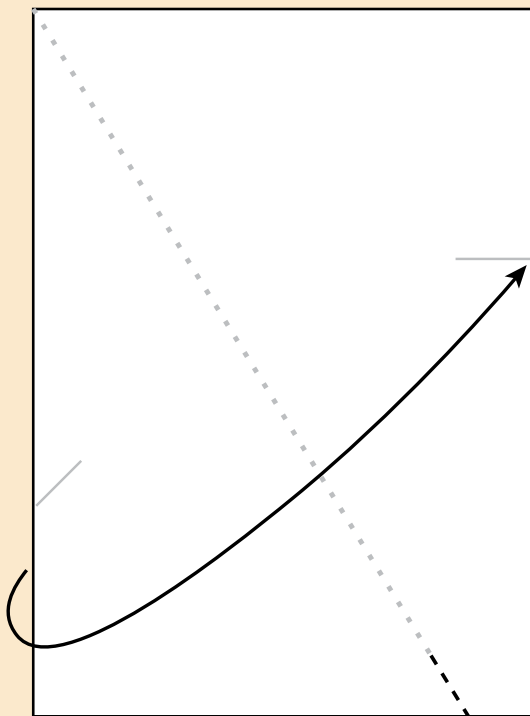
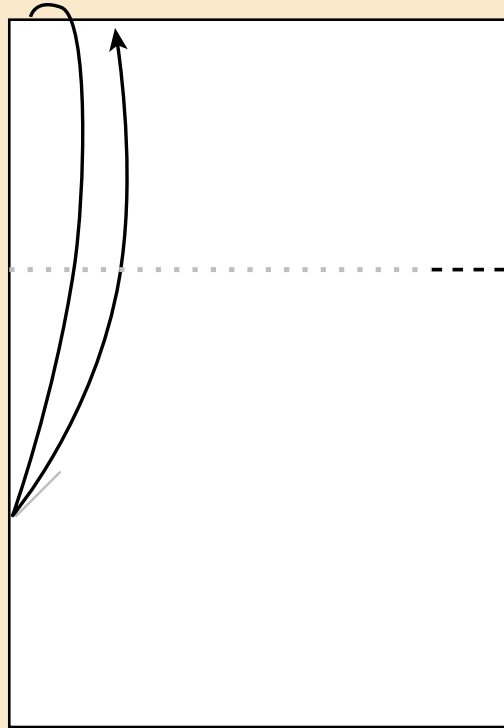
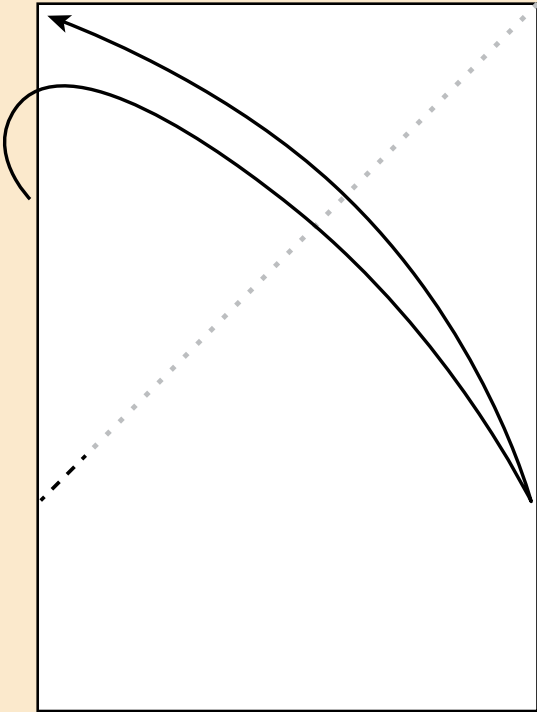
**The golden rectangle is also found in nature and used in art because it is thought to be visually pleasing and harmonious.*

In the following chapter we will convert square and rectangle papers into golden rectangles.

Golden Rectangle from a Square

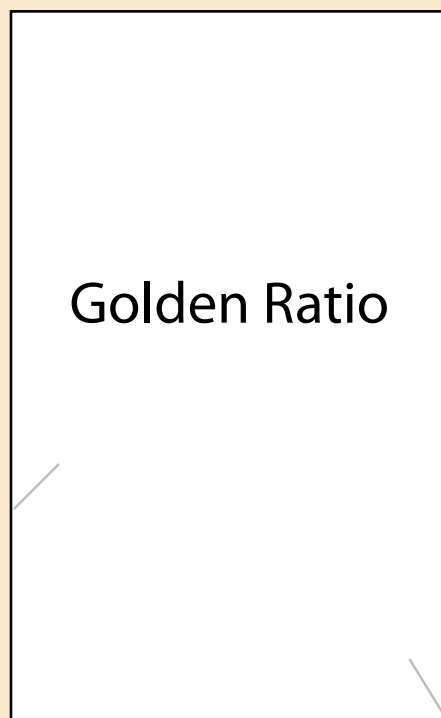
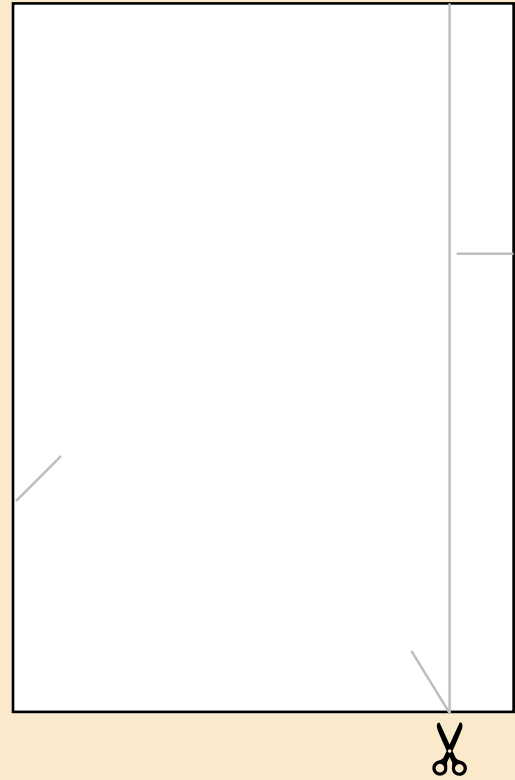
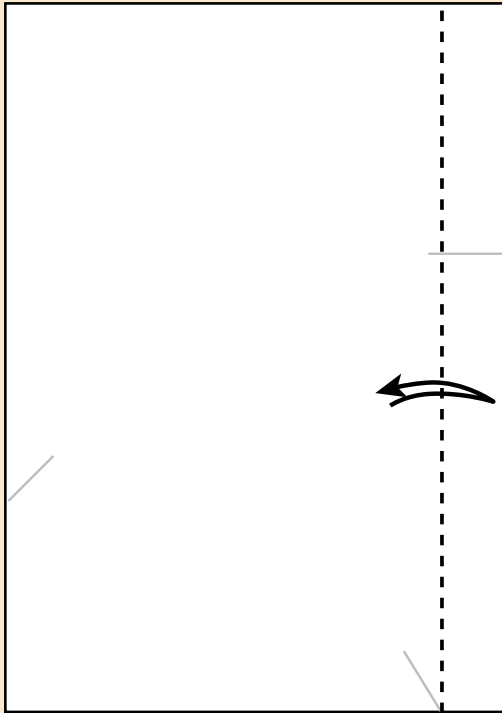


Golden Rectangle from any Rectangle



Pinch
here

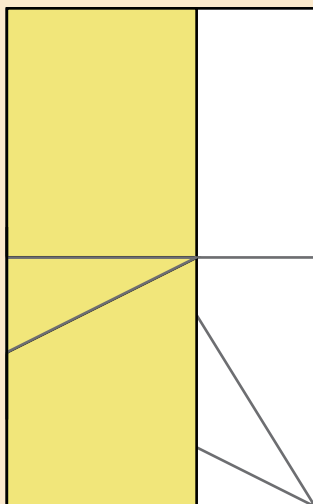
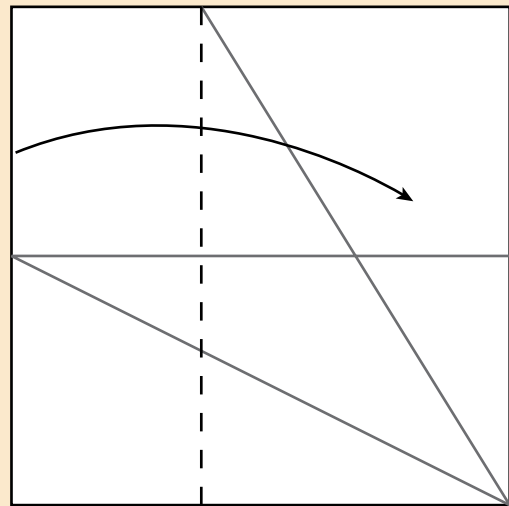
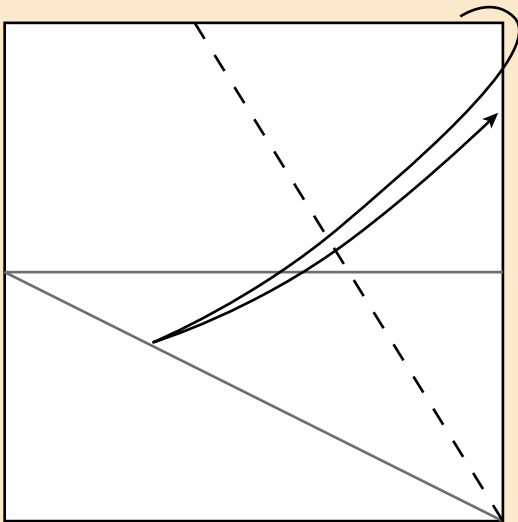
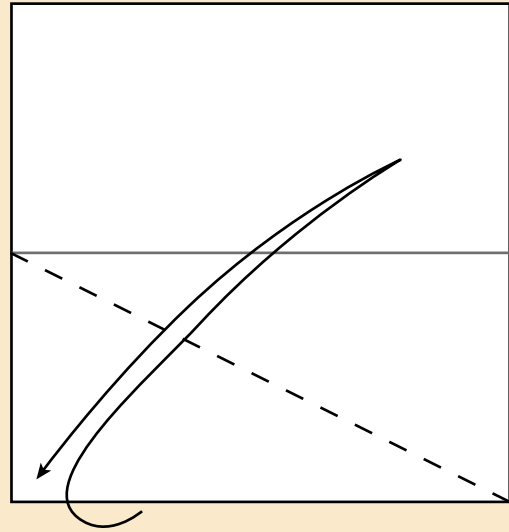
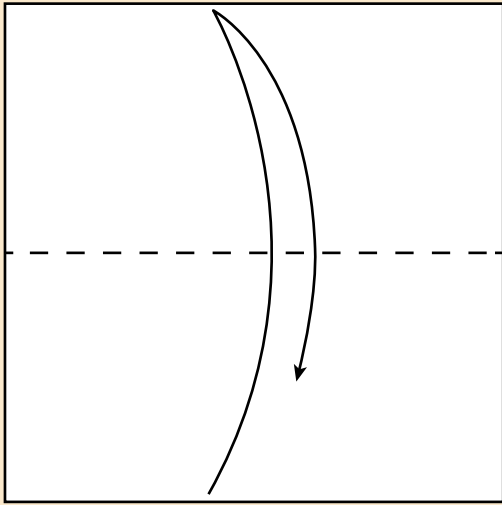




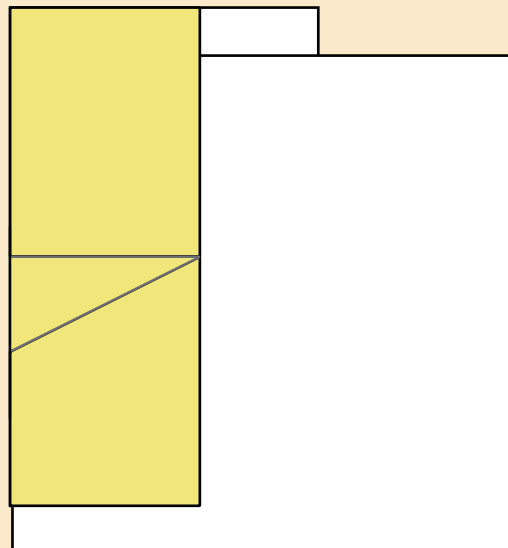
Discard



Creating 6 Golden Rectangles from a Square

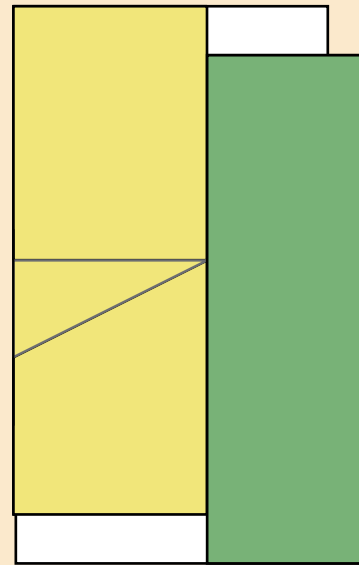
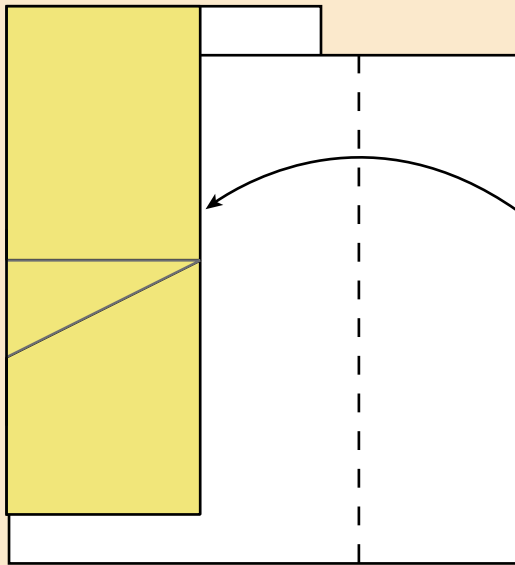


Template is ready

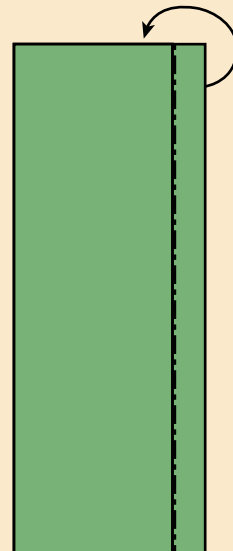
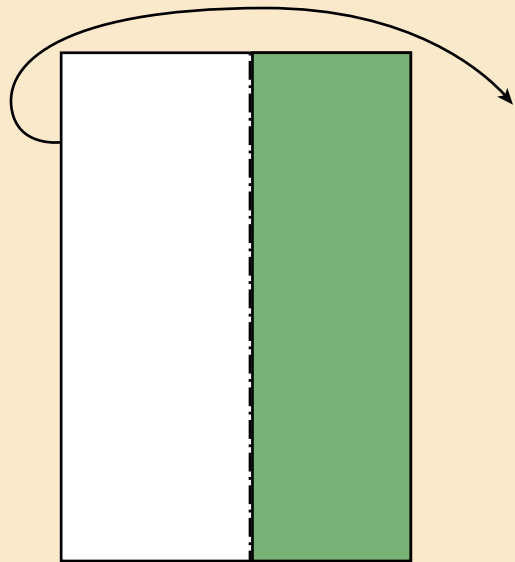


Place a second sheet into the template

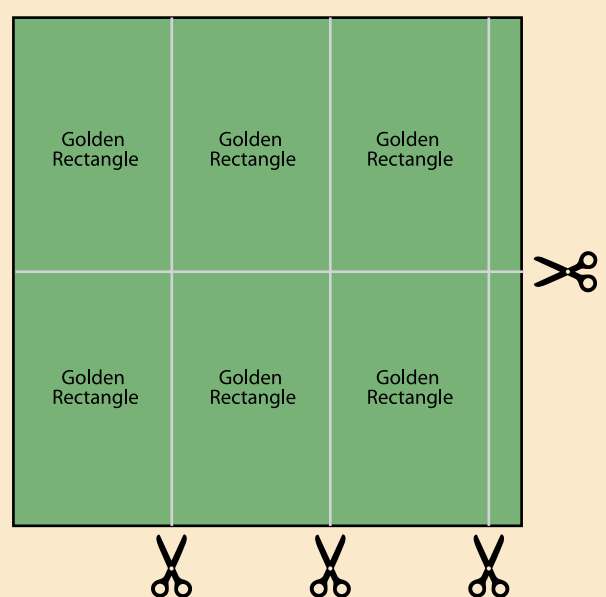
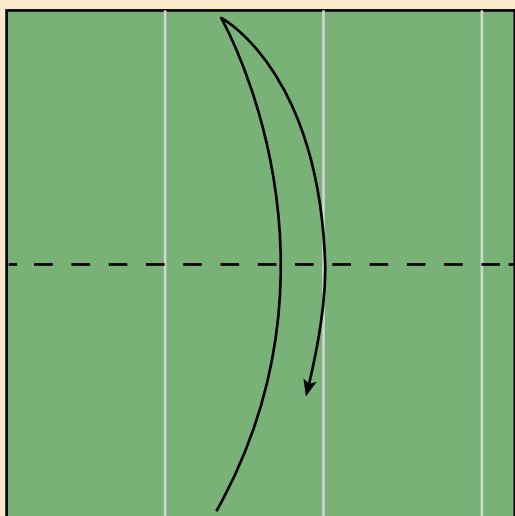




Take sheet out of the template

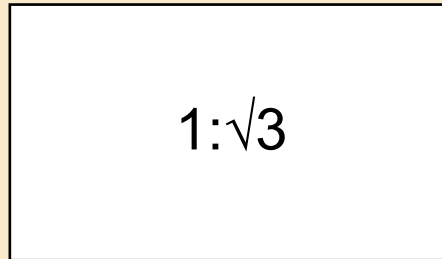


Open completely



Bronze Rectangle

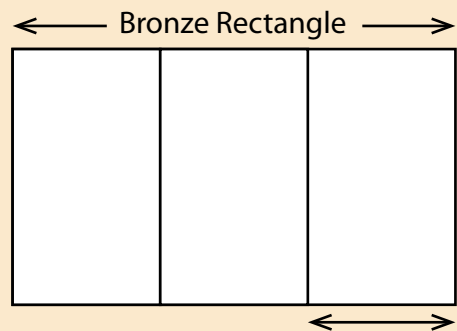
Bronze rectangles are often used in origami for making shapes with 30° , 60° or 120° angles. The ratio of the width to length of a bronze rectangle is $1:\sqrt{3}$.



Bronze Rectangle

Special Property

If you cut the bronze rectangle into thirds, the resulting pieces are also of the ratio $1:\sqrt{3}$.

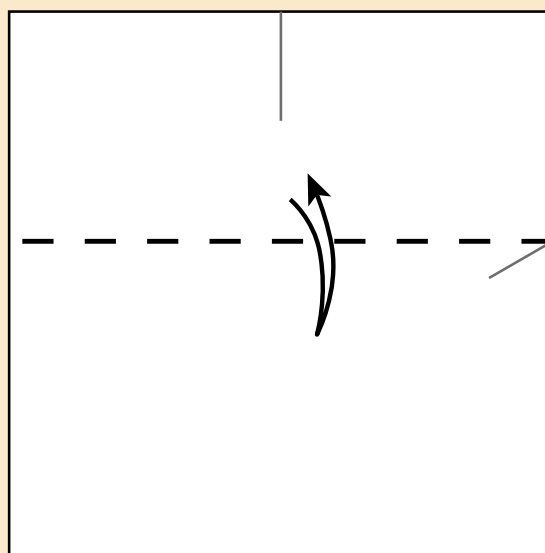
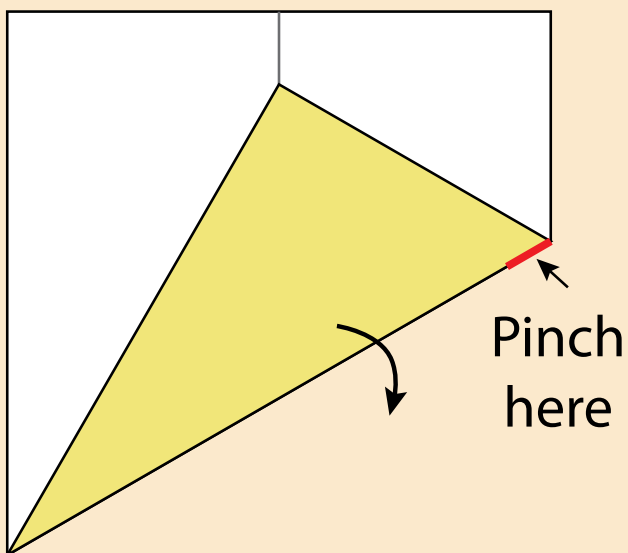
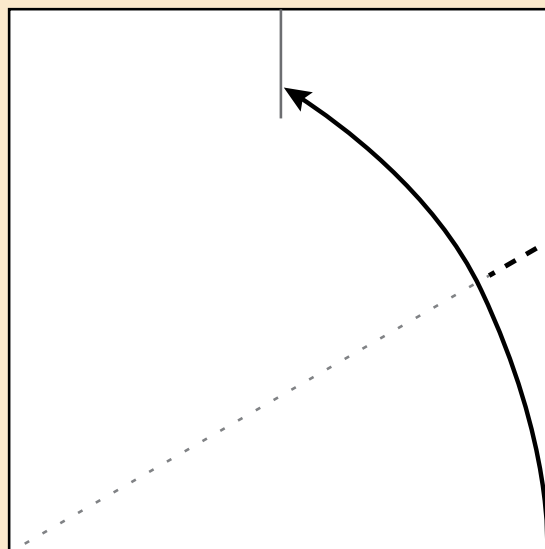
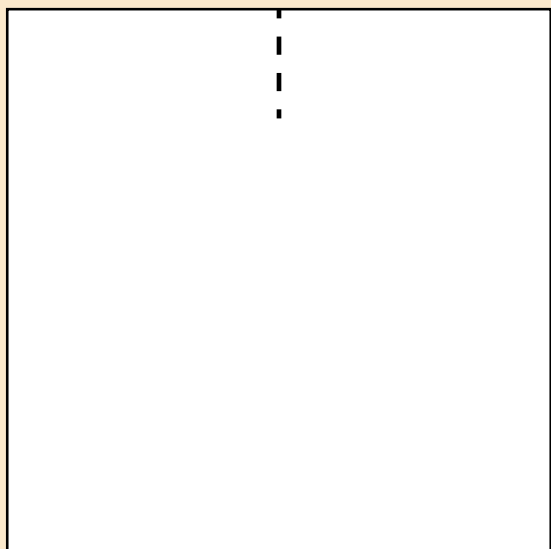


Bronze Rectangle

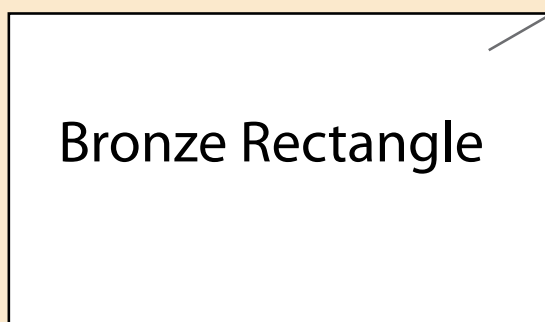
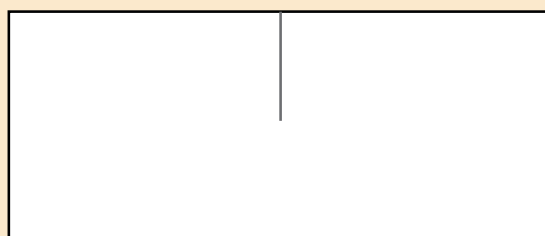
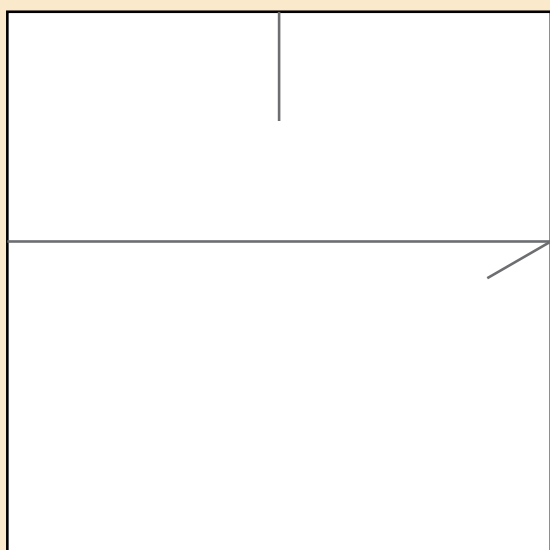
**Origami equilateral triangles, tetrahedra, and icosahedra often use the creases from a bronze rectangle.*

In the following chapter we will convert square and rectangle papers into bronze rectangles.

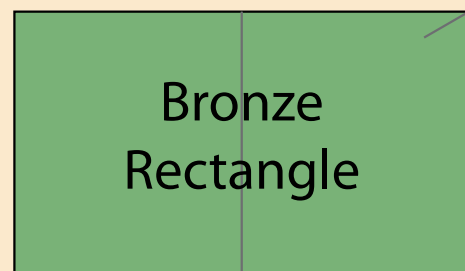
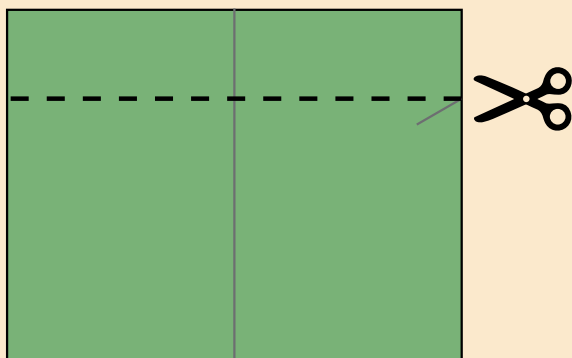
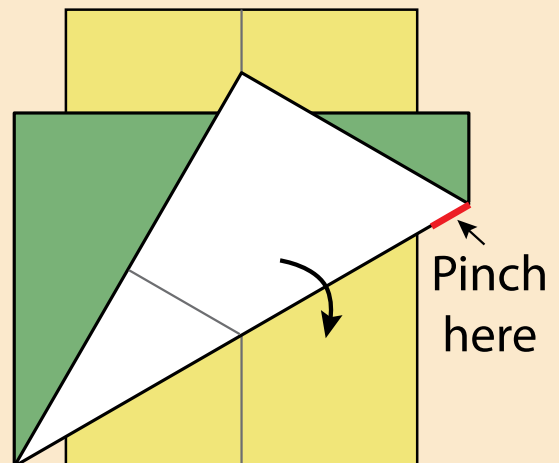
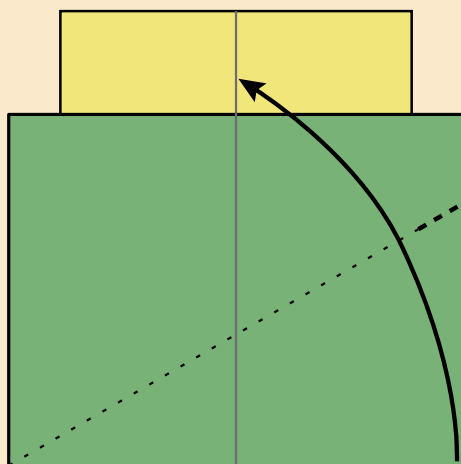
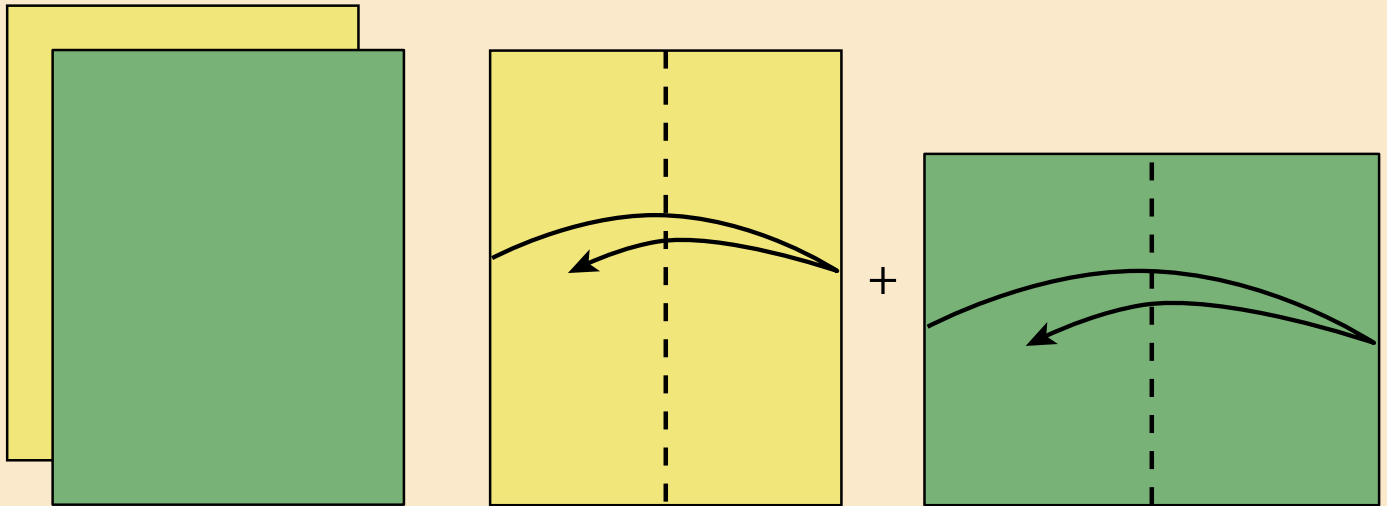
Bronze Rectangle from a Square



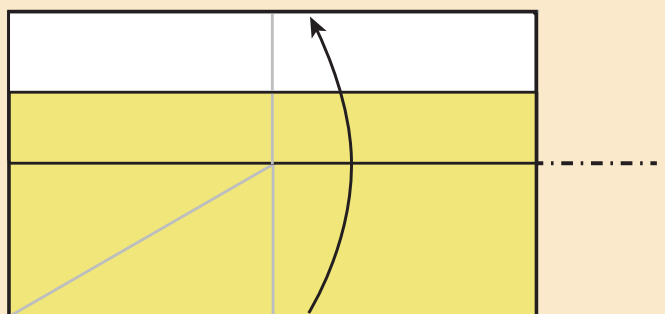
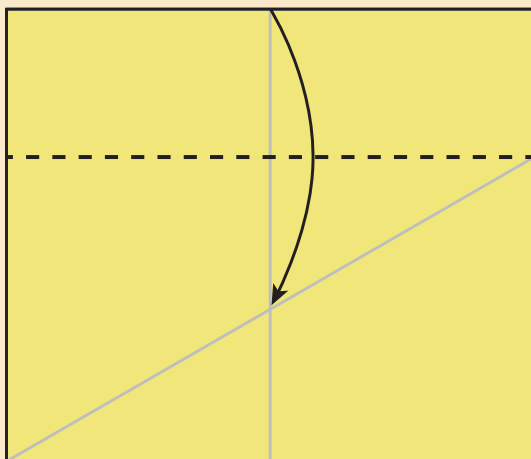
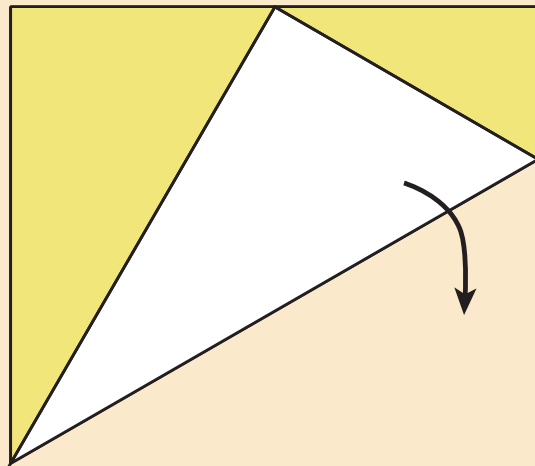
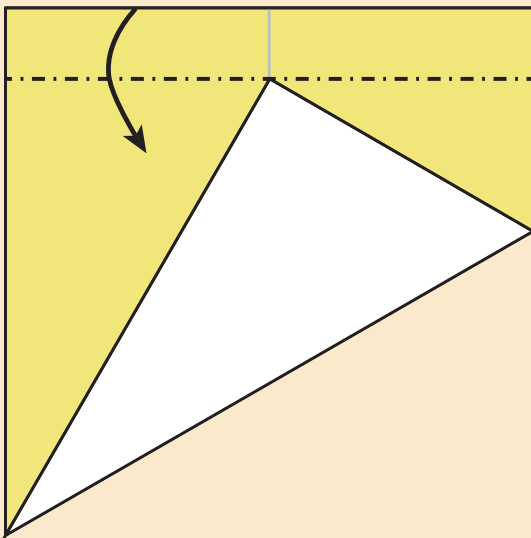
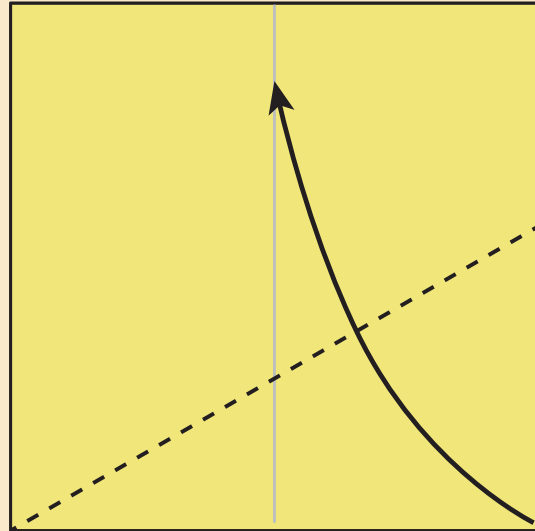
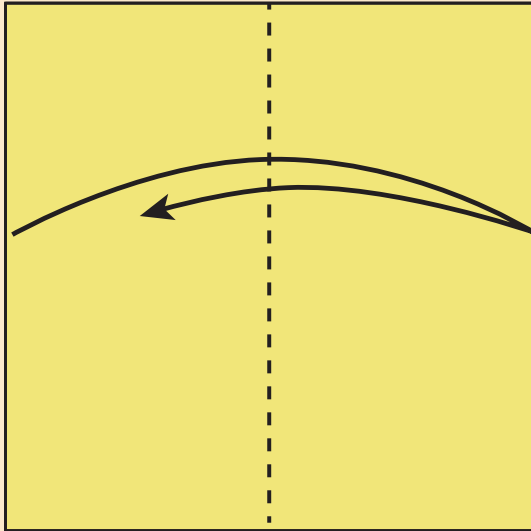
Discard

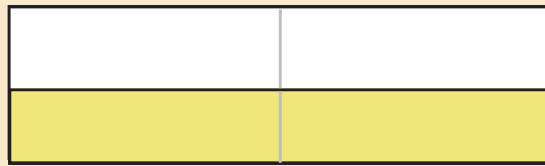


Bronze Rectangle from a Rectangle

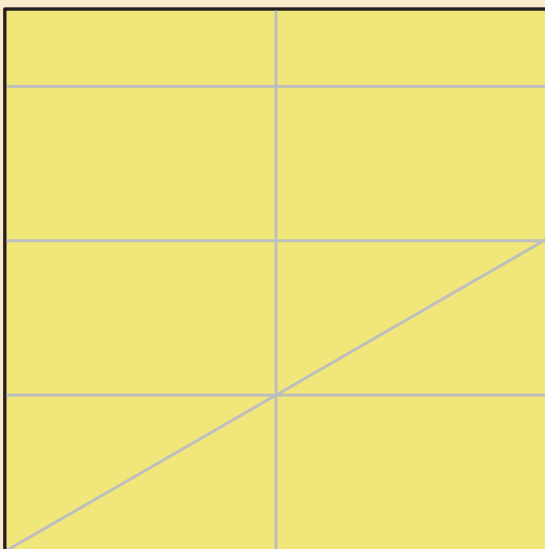


Creating 6 Bronze Rectangles from a Square





Open all

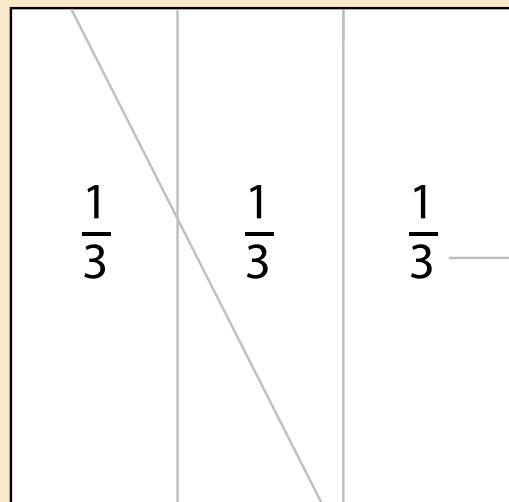
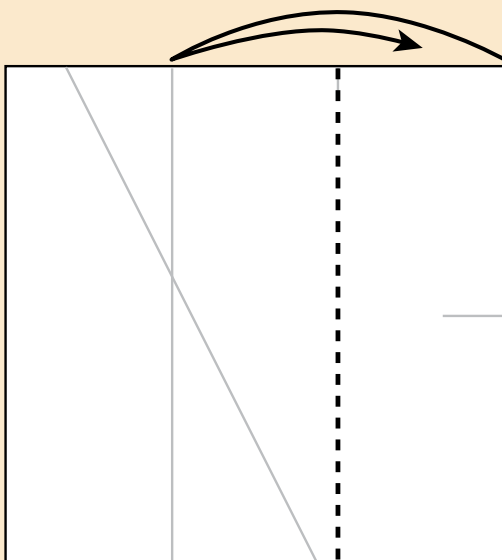
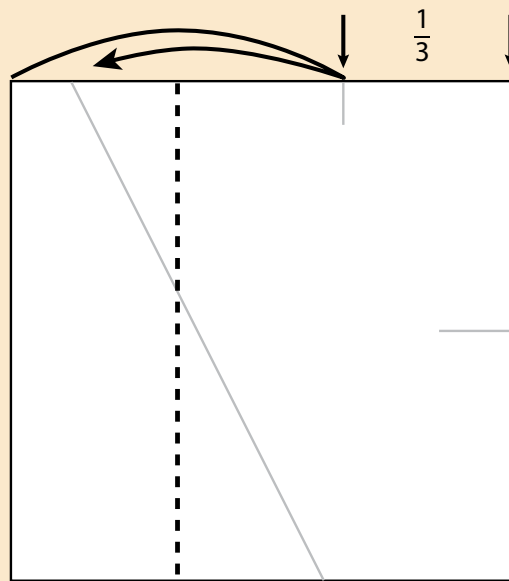
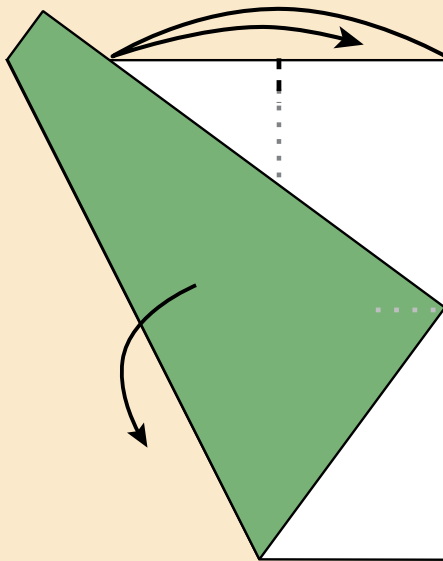
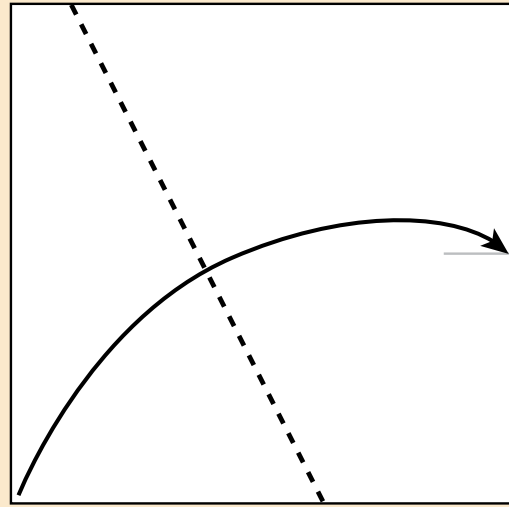
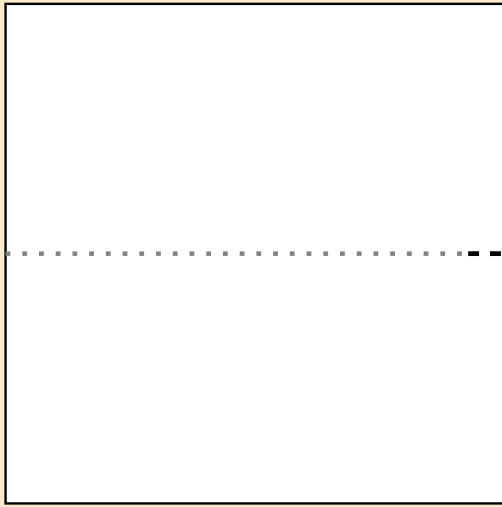


Paper Divisions

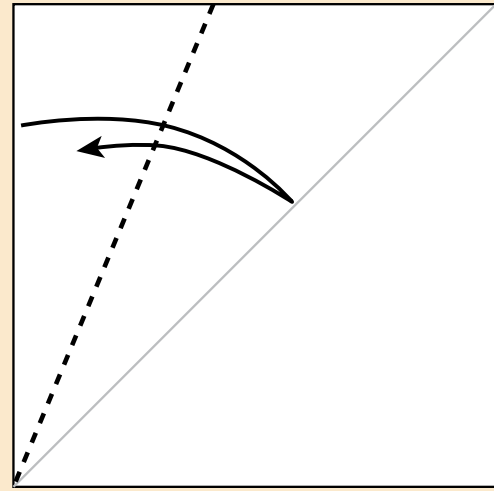
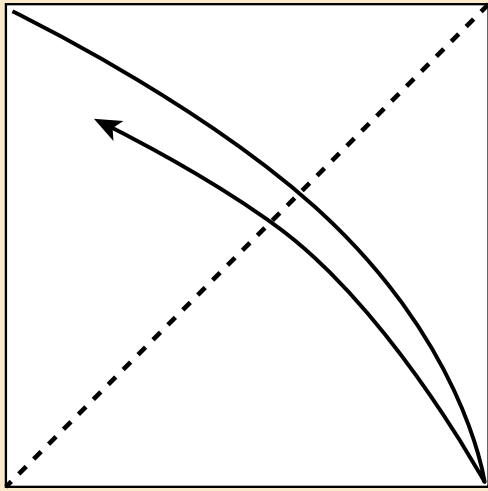
Sometimes in origami we need to divide our papers by an uneven number. Of course, we can always use a ruler, a sheet of second paper with lines or even the “s” method. The best and most accurate way will always be the origami-way.

In the following chapter we will divide a square into thirds and fifths by using creases.

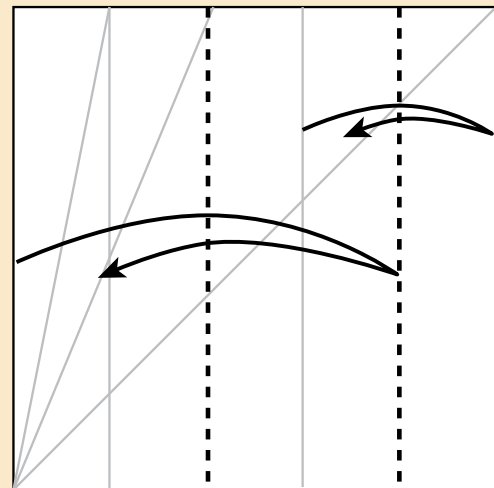
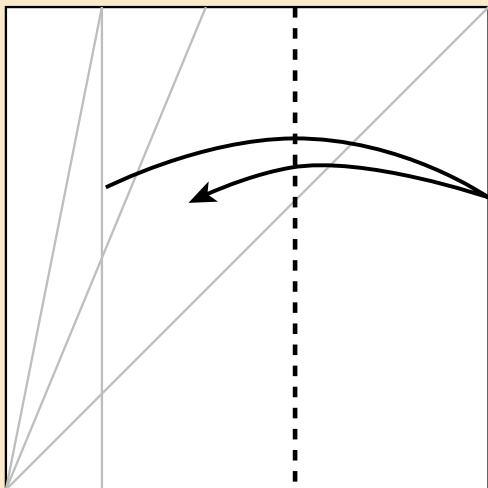
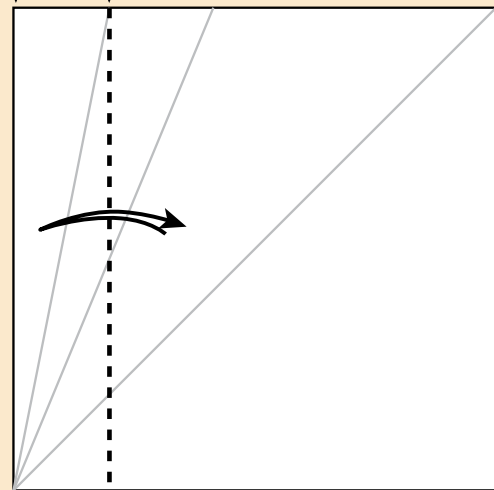
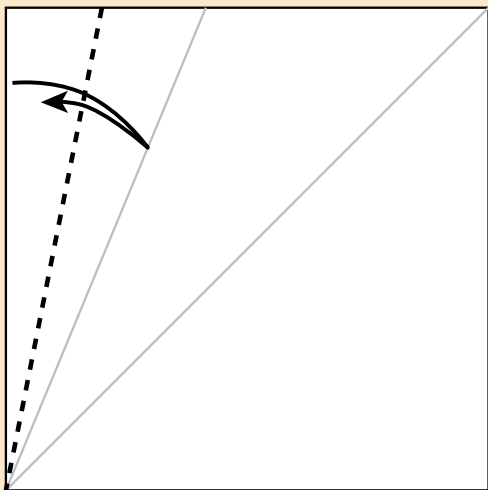
Divide a Square into Thirds



Divide a Square into Fifths



$\frac{1}{5}$



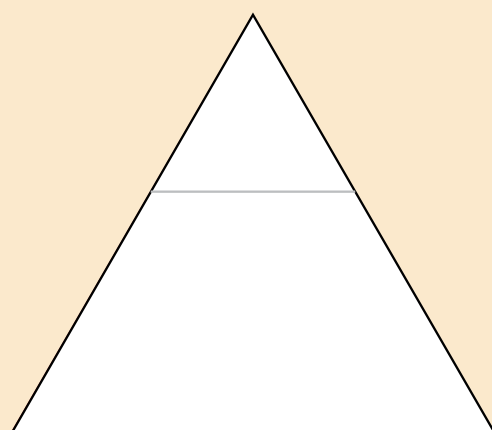
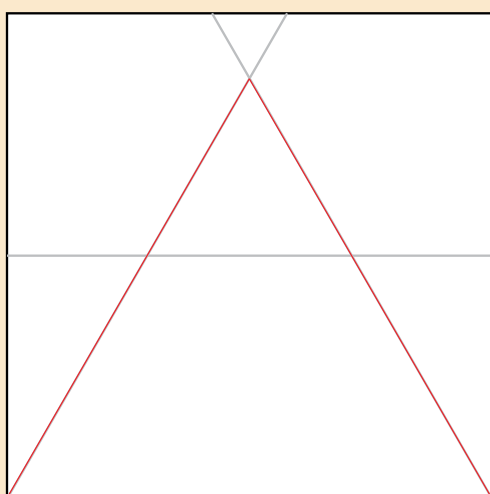
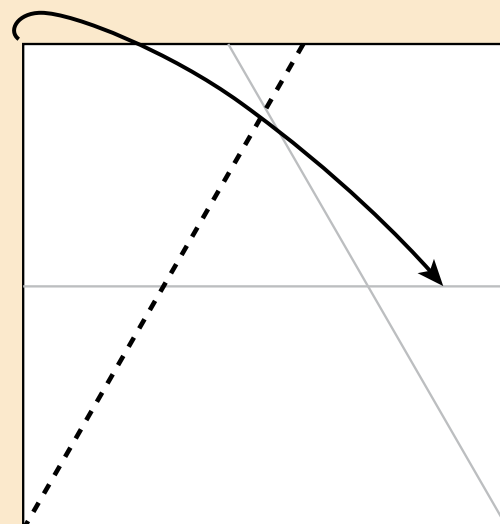
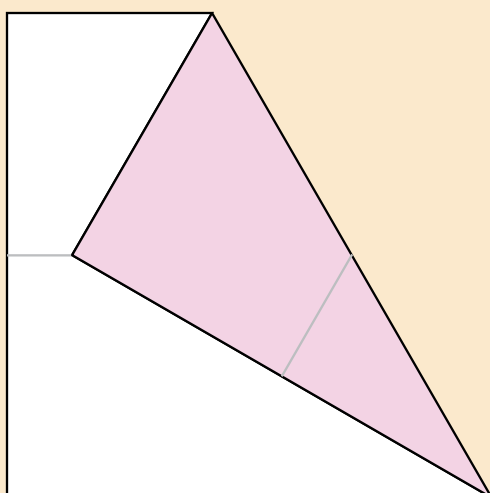
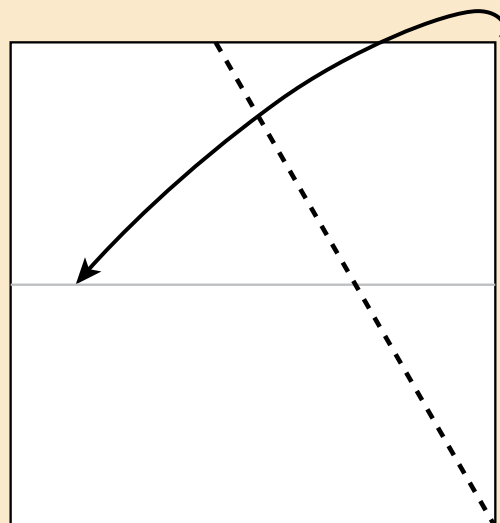
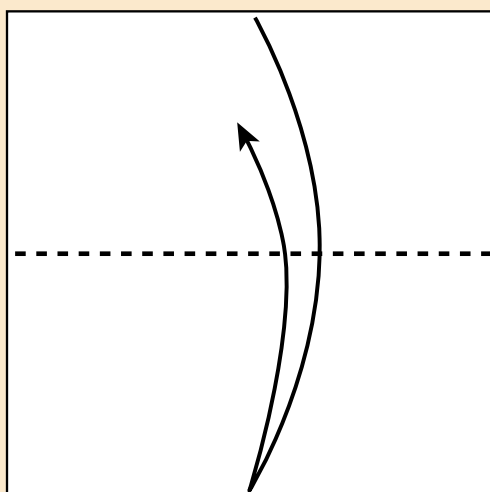
Paper Shapes

Sometimes in origami we need to cut various geometric shapes. Using origami methods always leaves creases on the final shapes. The best way to get a clean, uncreased, paper is by making a template.

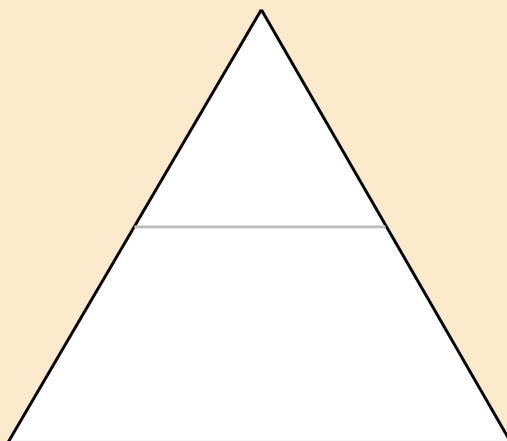
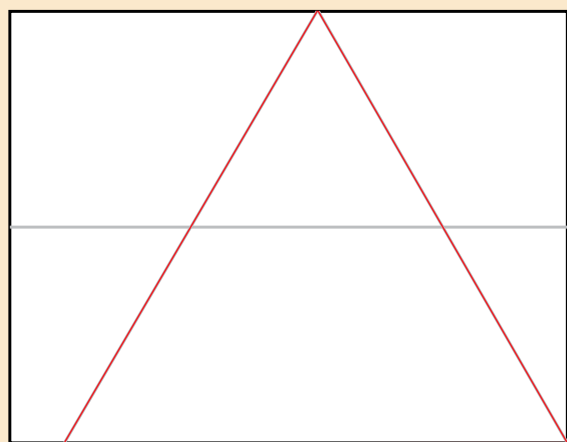
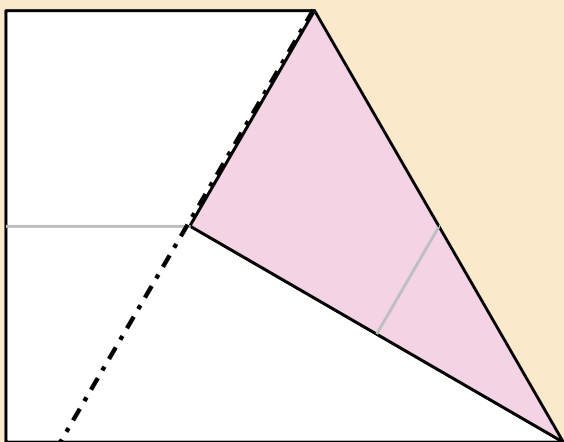
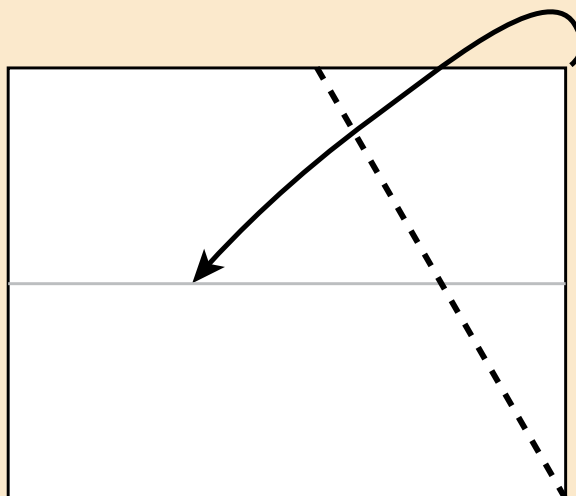
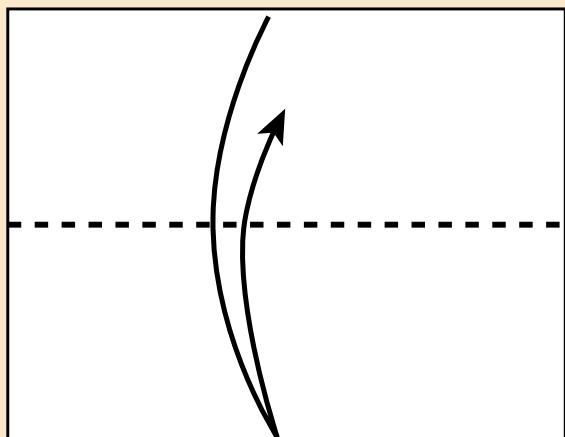
If possible, purchase metal templates, these will give you the best and most accurate results.

In the following chapter we will cut the “most used shapes” in origami from square and rectangle papers.

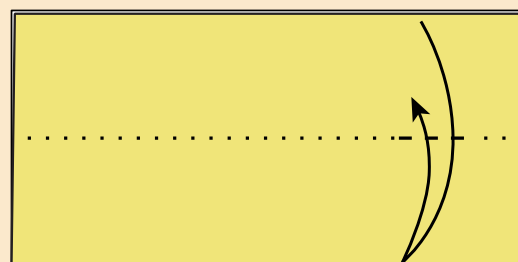
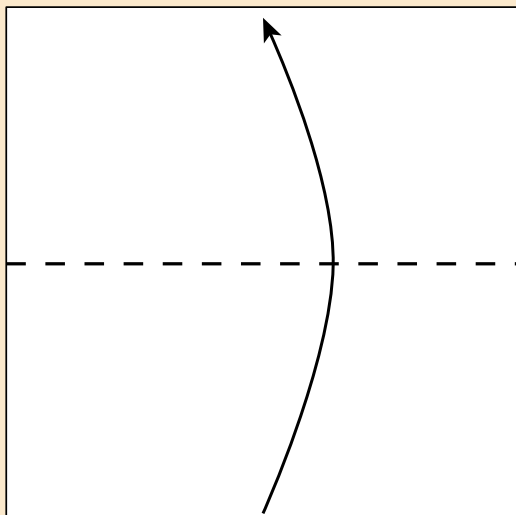
Equilateral Triangle from a Square



Equilateral Triangle from a Rectangle



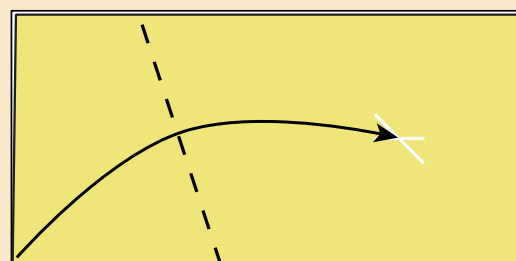
Pentagon from a Square



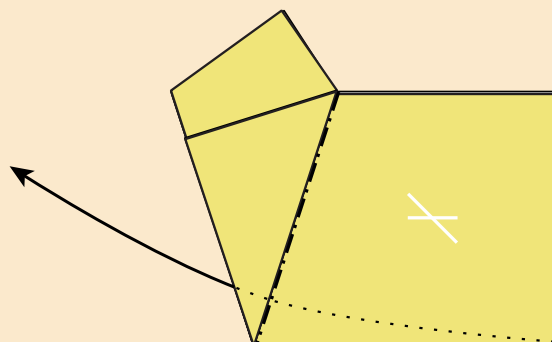
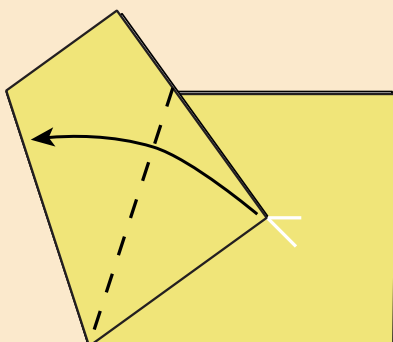
Pinch (top layer)
only where indicated



Pinch (top layer)
only where indicated

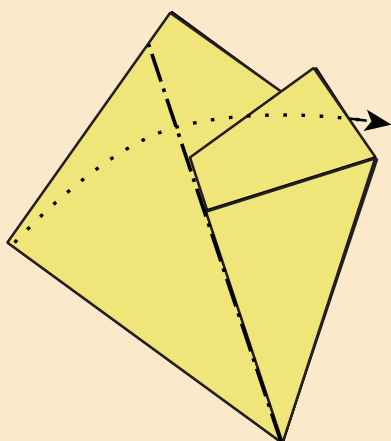


Bring the corner
to the pinches intersection

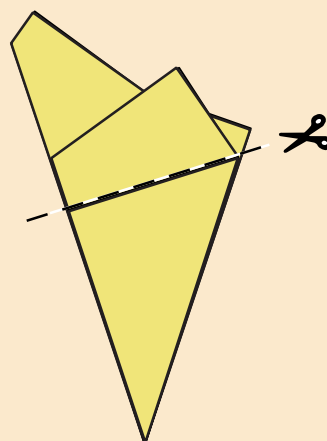


Mountain fold along the edge

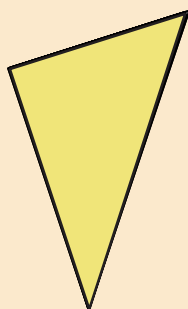




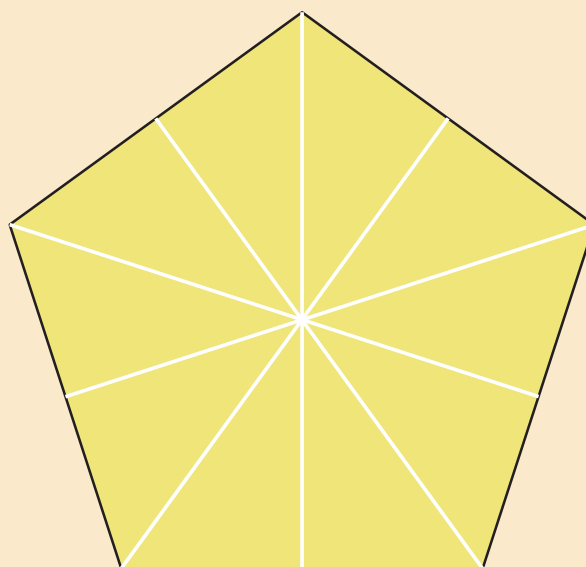
Mountain fold along the edge



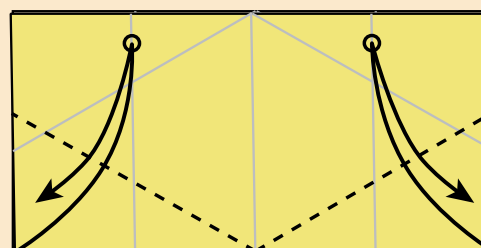
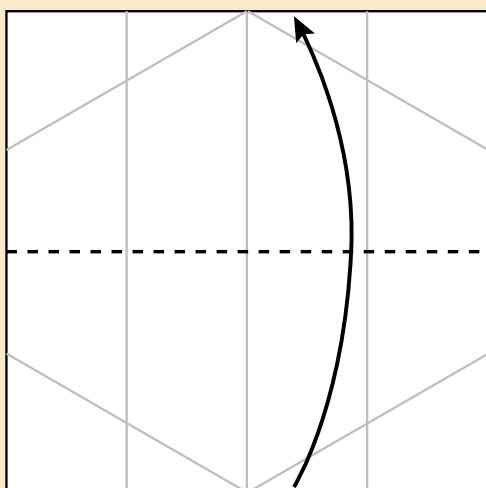
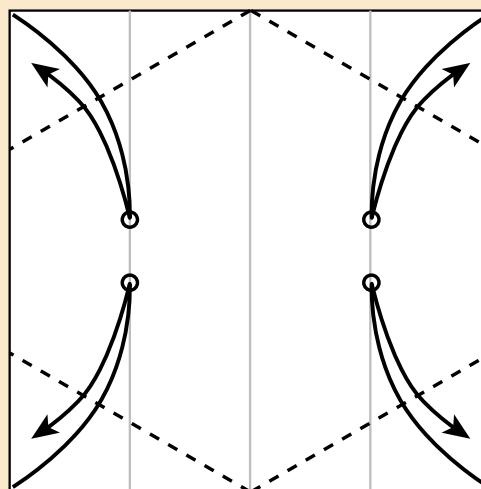
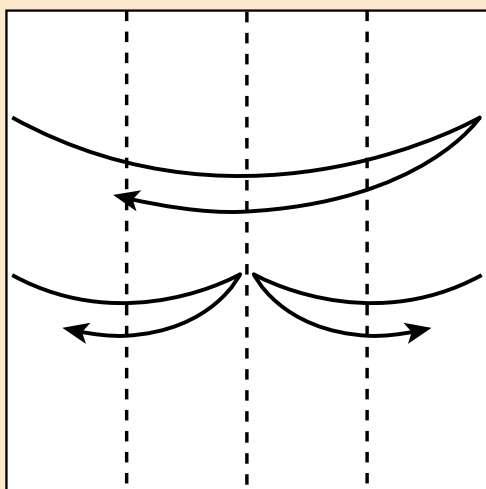
Cut along the edge



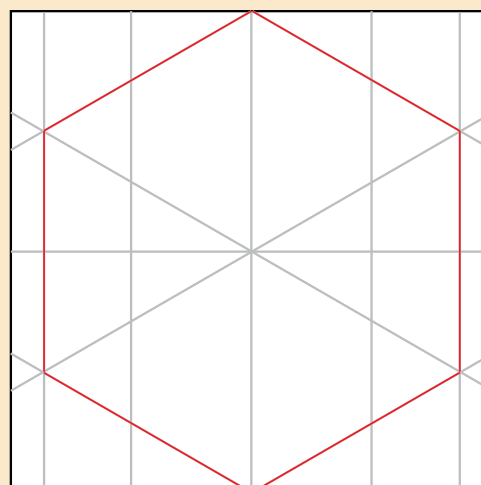
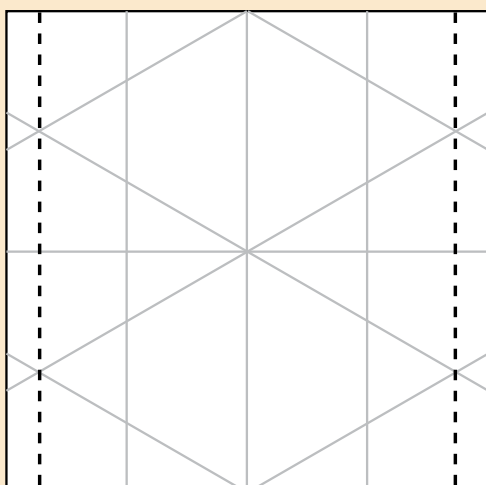
Open everything



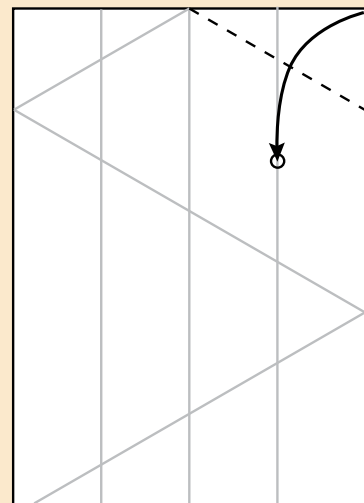
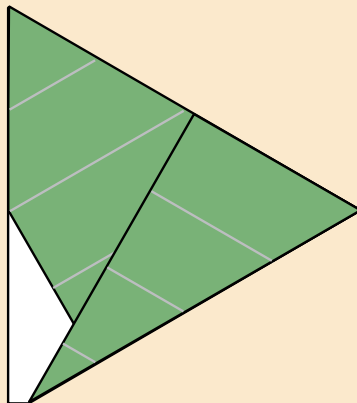
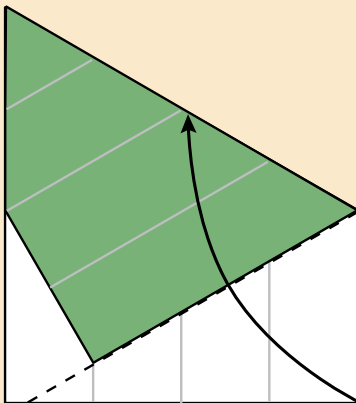
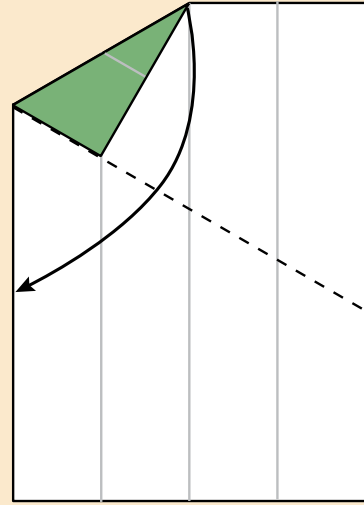
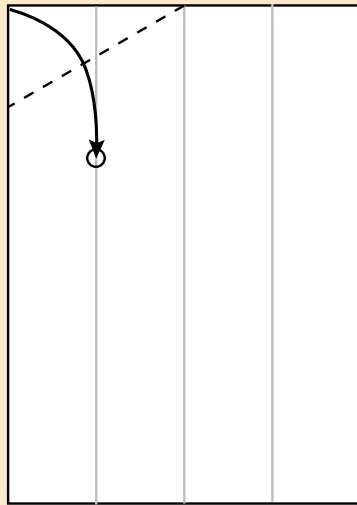
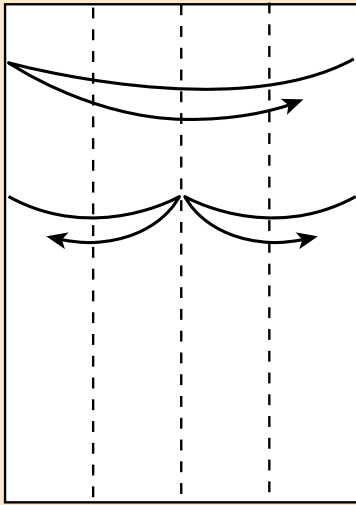
Hexagon from a Square



Fold the corners as shown.
Unfold everything



Hexagon from a Rectangle



Repeat steps 2-5 starting from the right corner

